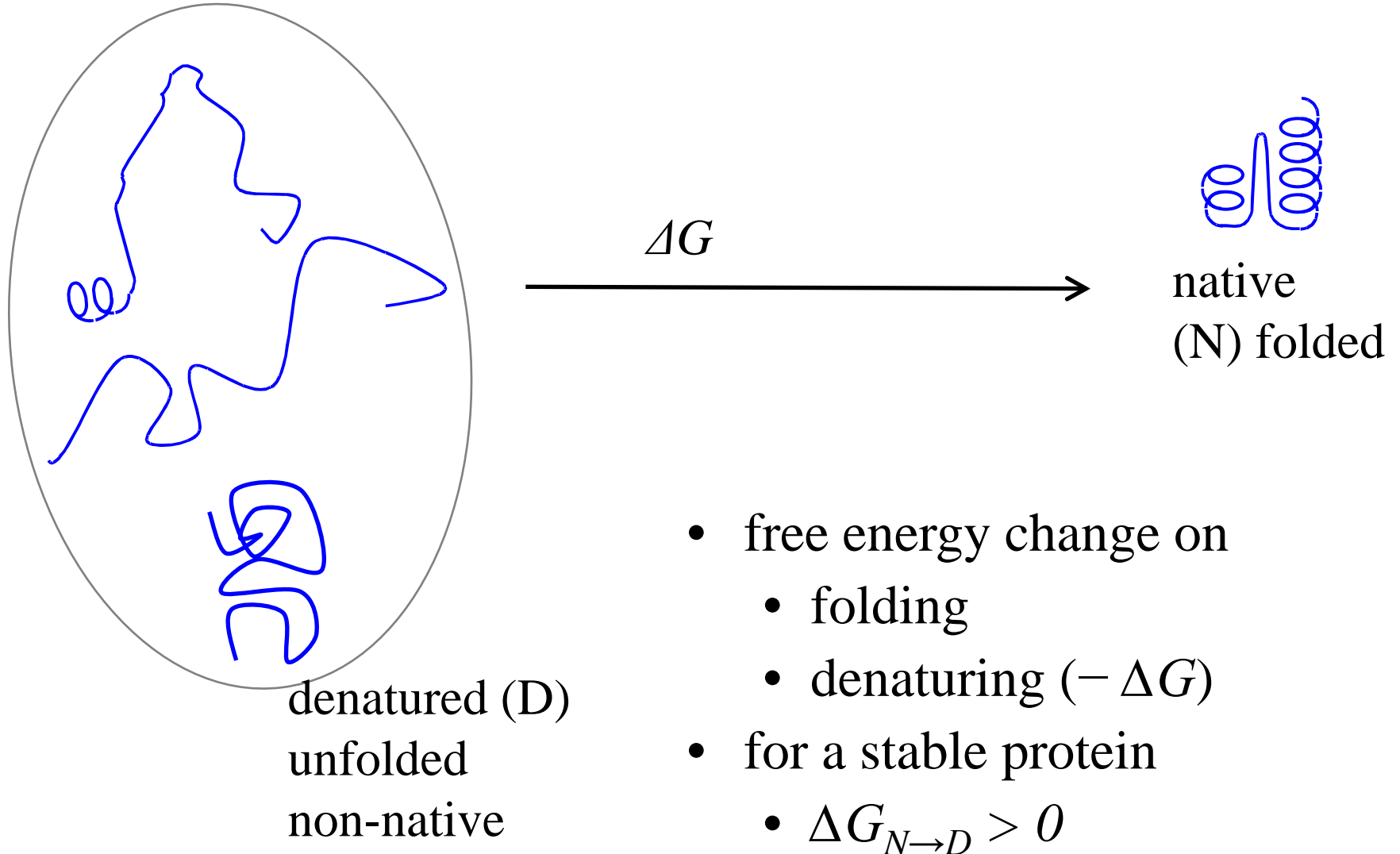


# Protein stability

Andrew Torda, Wintersemester 2009 / 2010, GST

- Our model



# Protein Stability

- what is known empirically
- definitions
- a stability surprise
- some explanations
- weaknesses of models

## $\Delta G$ convention

- $\Delta G_{folding} = - \Delta G_{unfolding}$
- define  $\Delta G > 0$  as stable so reaction is
  - folded  $\rightarrow$  unfolded (native  $\rightarrow$  denatured)
- some books and papers work with other convention

# Empiricism / rules

- more positive  $\Delta G$ , more stable the protein
- most proteins are marginally stable ( $\Delta G \approx 0$ )
- proteins can be denatured by
  - pH, concentrated ions, temperature, solvent, surface area
- too hot ?
  - eggs cook, people die (many reasons)
- some bacteria live at 373 K – their proteins are not denatured

# Rules

- nature cares about free energy  $\Delta G$ 
  - usually measure free energy
  - $\Delta G = \Delta H - T \Delta S$ 
    - $G$  free energy (Gibbs)
    - $H$  enthalpy  
potential energy including volume effects  $U + PV$
    - $S$  entropy
- chemistry books normally work with  $\Delta G$  standard free energy

# measurement

## Folded / Unfolded

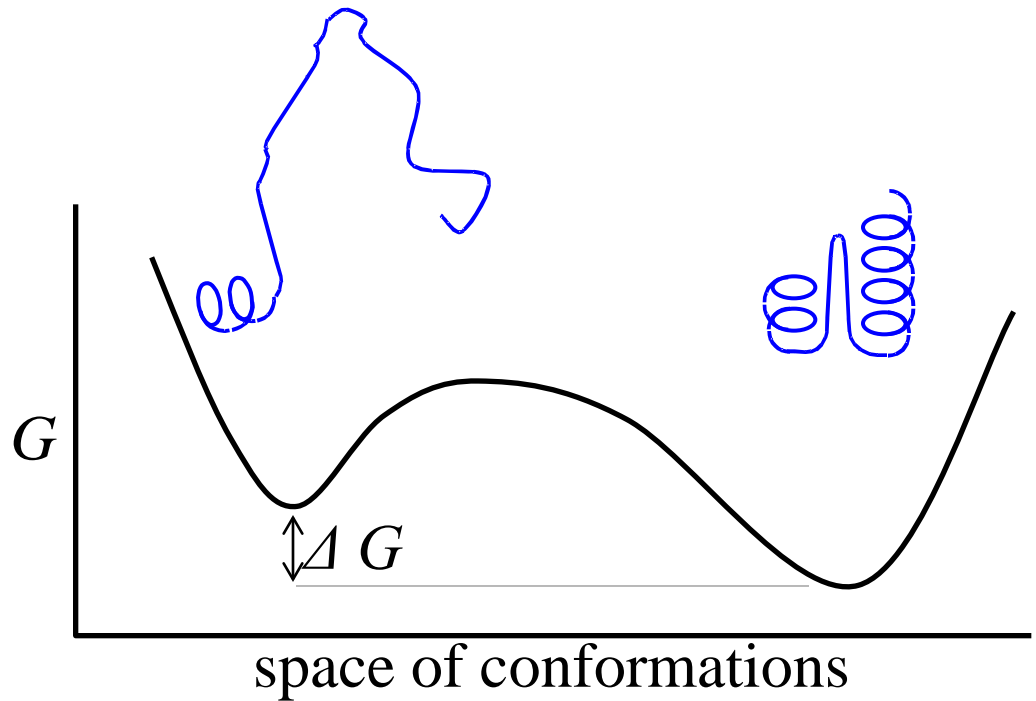
- how to measure
  - spectroscopy
    - absorbance (optical / UV spectroscopy)
    - rotational (CD / ORD)
    - fluorescence
    - NMR
  - activity
  - ...
- usually – two states (native / denatured) that somehow look different

## Energies

- calorimetry
- measurements of [native] / [denatured]

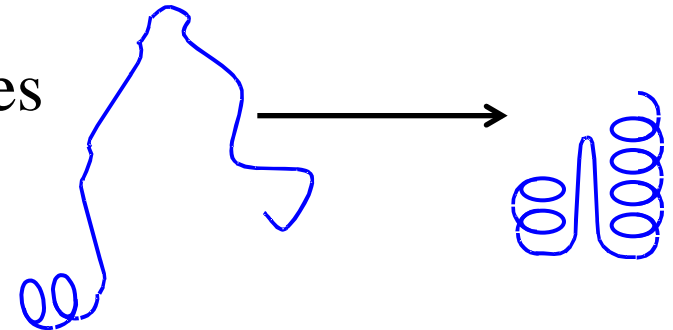
# Two state model

- model requires an energy barrier
- what if  $\Delta G = 0$ 
  - 1/2 molecules folded
  - 1/2 molecules denatured



# First picture of stability

- what holds a protein together ?
  - forces between atoms
    - bonds, electrostatic, Lennard-Jones
  - atoms also repel
- cannot be so simple
  - atoms would just fall into correct position
  - $\Delta G$  would always be very positive
  - missing ?
    - effect of solvent
- in native structure there are "correct contacts"

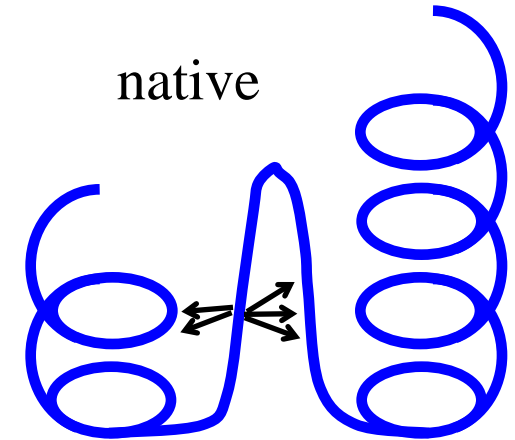


# Balance of energy terms

- in native structure there are correct contacts

One atom in native structure

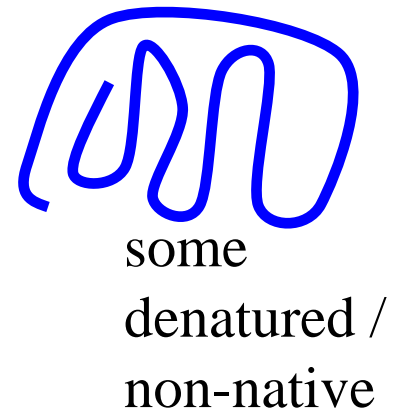
- interacts with correct neighbours



In the non-native structures there are also contacts

- atom interacts with “wrong” neighbours

- balance of forces
- stability has to do with
  - energy / enthalpy  $H_{\text{native}} - H_{\text{denatured}}$

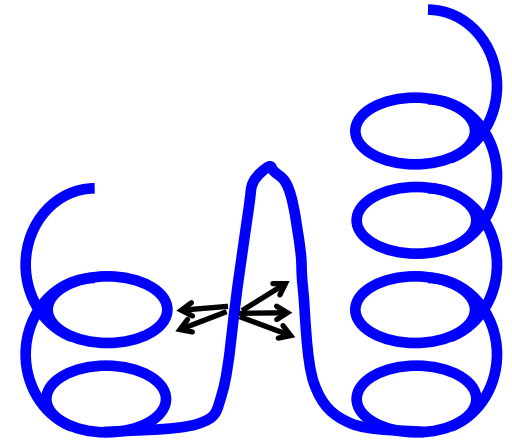




# Balance of energy terms

## More forces

- how many polar / charged groups are there ?
  - NH + CO backbone every residue
  - polar / charged sidechains
- all can interact with water
- stability will depend on  $H_{\text{native}} - (H_{\text{denatured}} + H_{\text{protein-H}_2\text{O}})$
- maybe  $H_{\text{native}} - H_{\text{denatured}}$  &  $H_{\text{native}} - H_{\text{protein-H}_2\text{O}}$

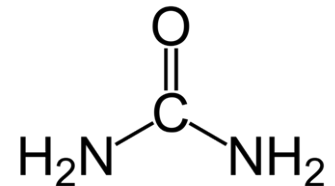
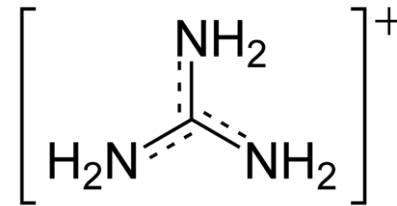


# Explain denaturing

Why do these denature a protein ?

pH, concentrated ions, temperature, solvent, surface area

- pH ? change the charge on some groups, remove favourable interactions
- ions ? provide competition for charges, H-bonds



- temperature ? add kinetic energy, push particles out of minima
- solvent ? remove favourable protein-solvent interactions
- surface area ? surface tension / protein –air interactions

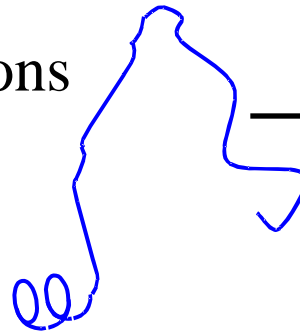
# Entropy version 1

$$\Delta G = \Delta H - T \Delta S$$

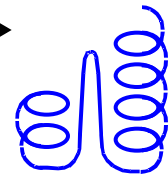
- considered  $\Delta H$  terms, what is  $\Delta S_{folded-unfolded}$  ?
  - entropy depends on the number of conformations ( $k \ln \Omega$ ) or

better  $-k \sum_{i=1}^{n_{states}} p_i \ln p_i$

lots of  
configurations



few  
configurations

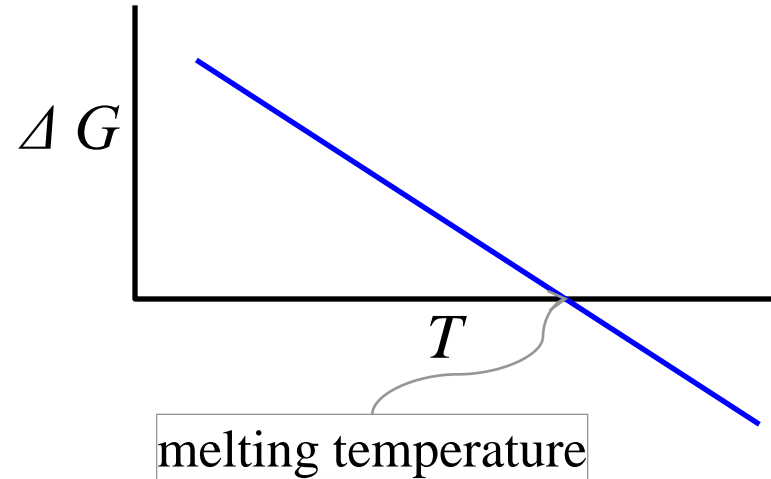
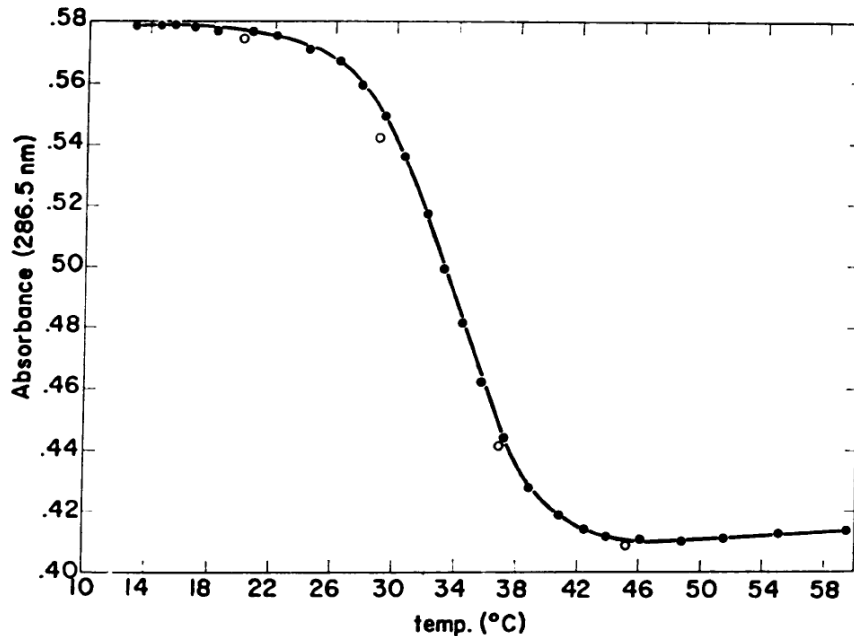


- as a protein unfolds
  - number of conformations  $\uparrow$
  - entropy goes  $\uparrow$
- $\Delta S$  will favour denaturing

# Balance of forces version 1

$$\Delta G = \Delta H - T \Delta S$$

- proteins should melt / cook / fall apart if you heat them



- ribonuclease unfolding

# Entropy version 2

$$\Delta G = \Delta H - T \Delta S$$

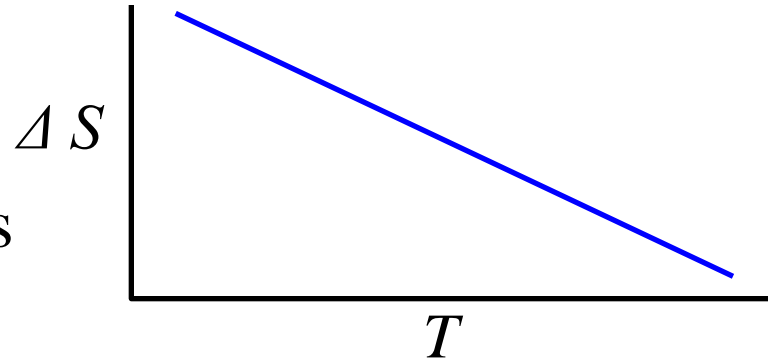
- but can we treat  $\Delta S$  as a constant ? Is it  $T$  dependent ?
- meaning of  $\Delta S_{folded-unfolded}$
- roughly how does the number of states change

$$\begin{aligned}\Delta S &= S_{folded} - S_{unfolded} \\ &= k \left( \ln \Omega_{folded} - \ln \Omega_{unfolded} \right) \\ &= k \ln \frac{\Omega_{folded}}{\Omega_{unfolded}}\end{aligned}$$

- $\Omega_{folded}$  definitely goes up with temperature
- related to heat capacity

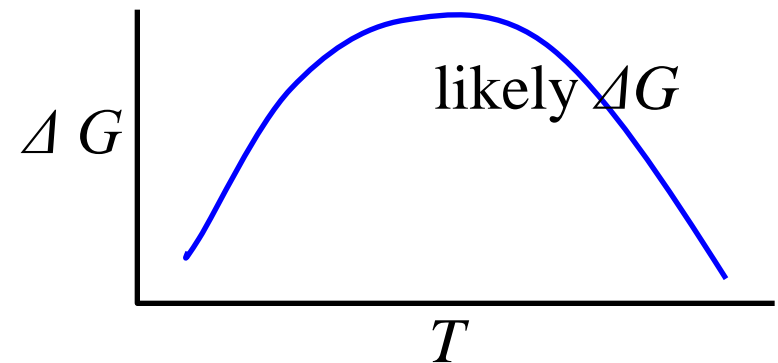
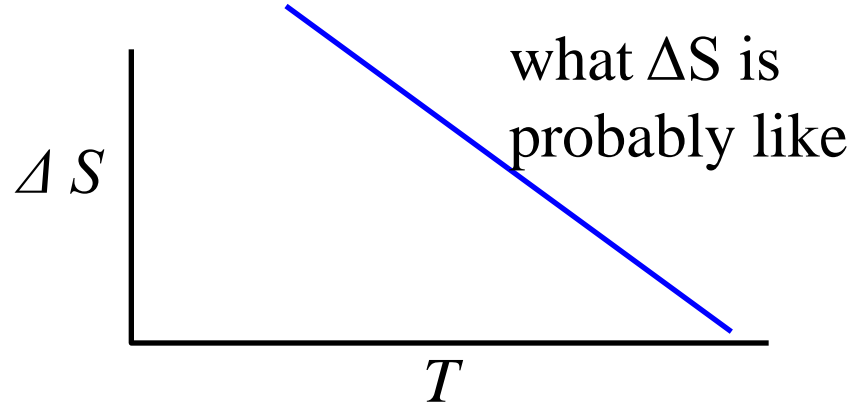
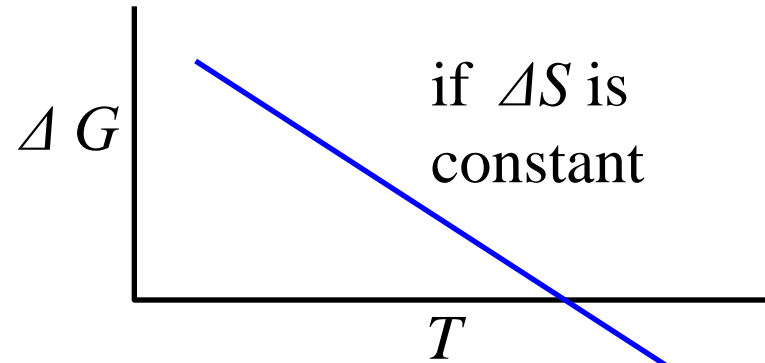
# Entropy change on unfolding

- depending on heat capacity one has a curve like
- radical consequence
  - entropy might make proteins less stable as you cool them
  - can you cook an egg by cooling it ?
- combining these properties



# protein stability

$$\Delta G = \Delta H - T \Delta S$$

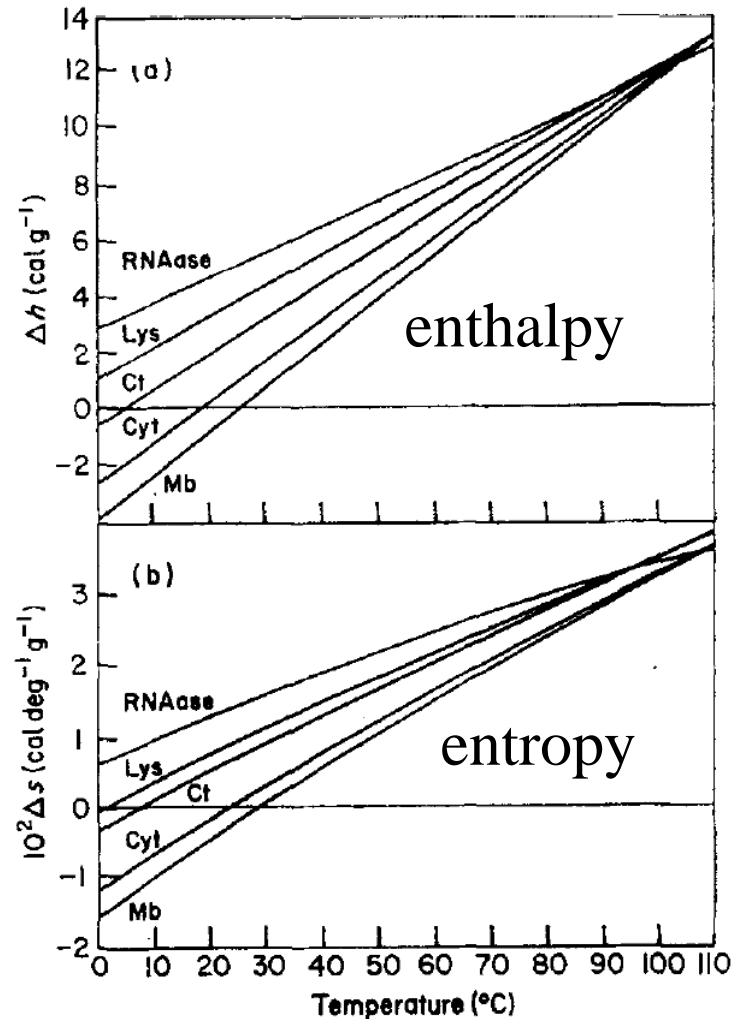


- what is seen / claimed ?

# Old measurements

- protein stability ( $\Delta G$ ) is a balance of energy and entropy
- note sign convention
$$\Delta G = \Delta H - T \Delta S$$
- difference of two large numbers comes to nearly zero
- what might you expect ?

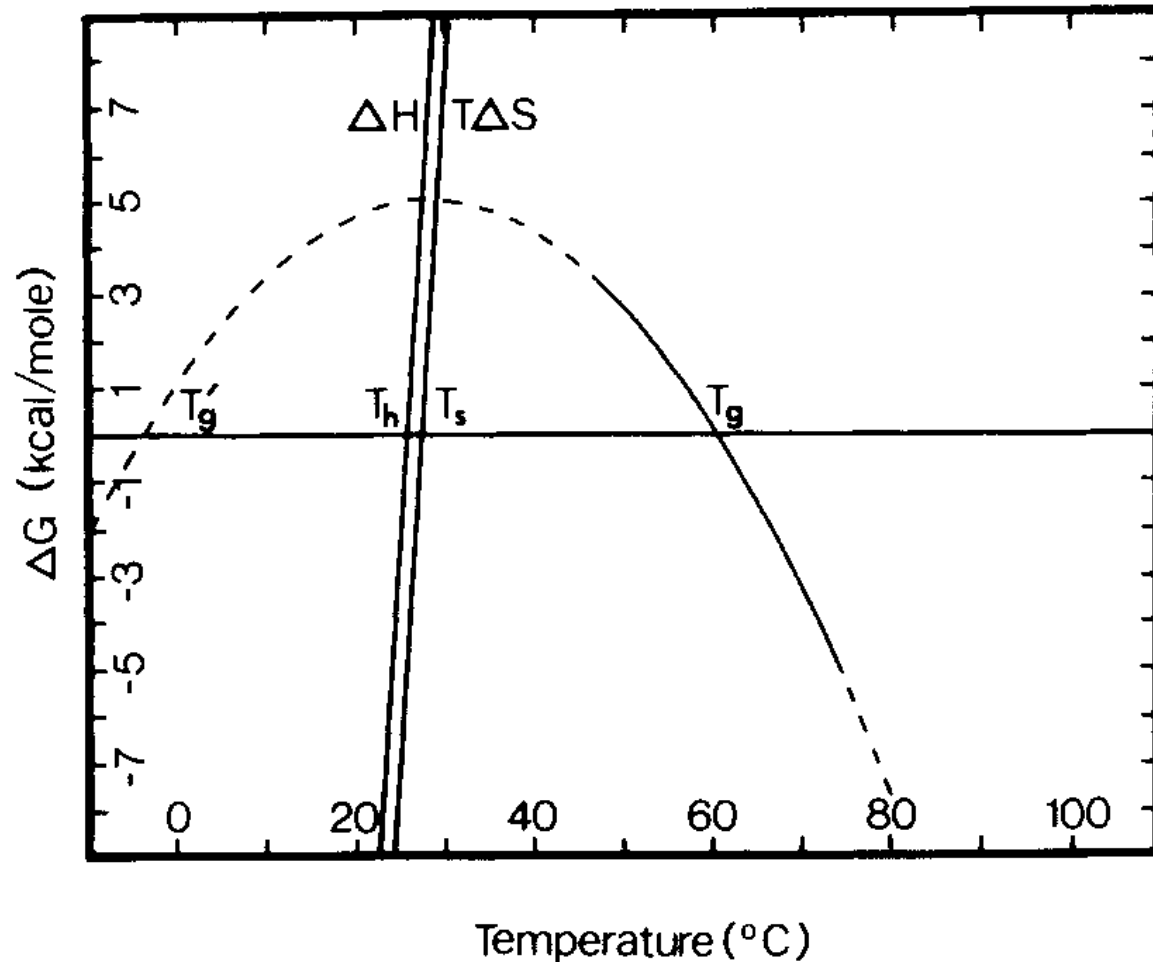
lysozyme  
RNAase  
chymotrypsin  
myoglobin  
cytochrome C





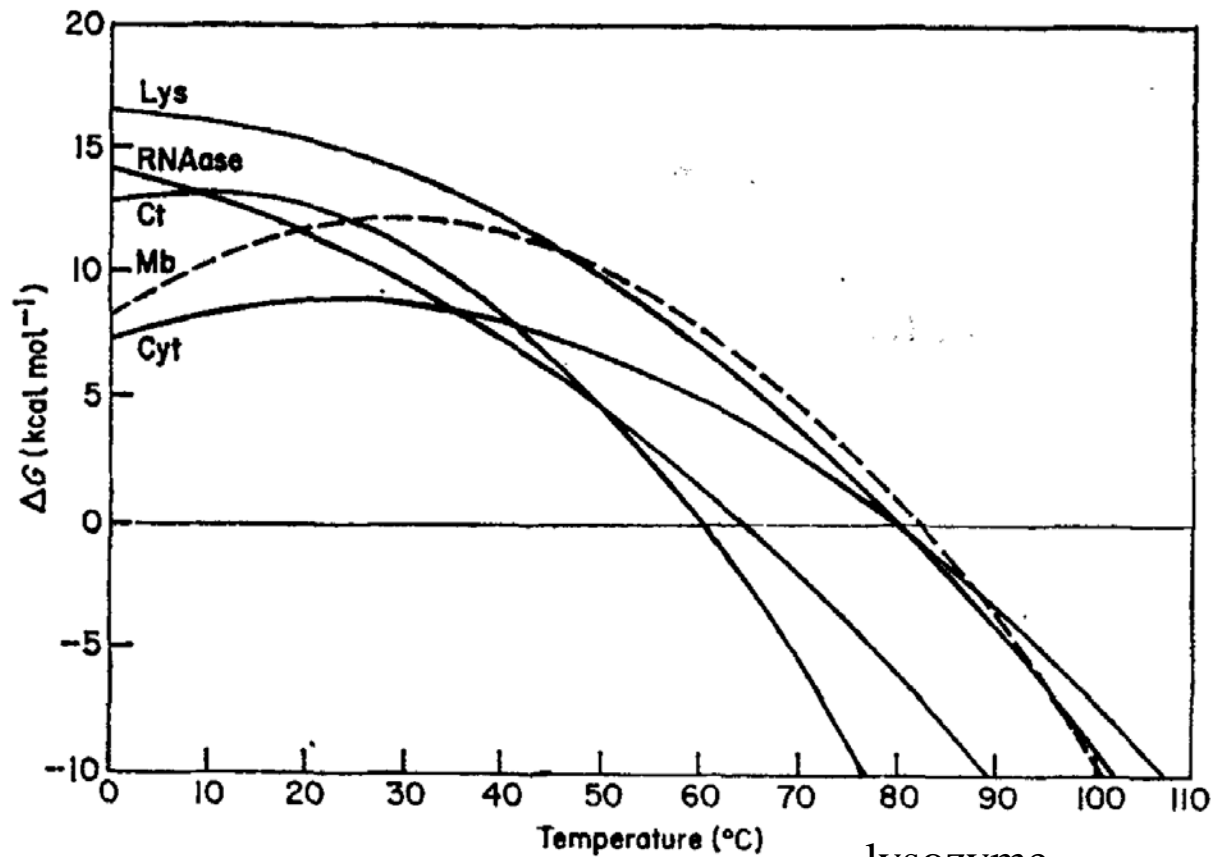
# final version

- claim.. for typical protein
- bold line –measured
- dashed – extrapolated
- implies
  - you can denature a protein by cooling (cook egg by freezing ?)
- what is measured



# free energy experimental

- Looks like there will be cold denaturing
  - below zero
- curve is different for all proteins
- does this prove "cold denaturing" ?



lysozyme  
RNAase  
chymotrypsin  
myoglobin  
cytochrome C

# Cold denaturing

- controversial
- often predicted to happen below 0
  - hard to measure

# Entropy and Enthalpy Summary / Consequences

Enthalpy  $H$  / potential energy

- will always favour folding

Entropy

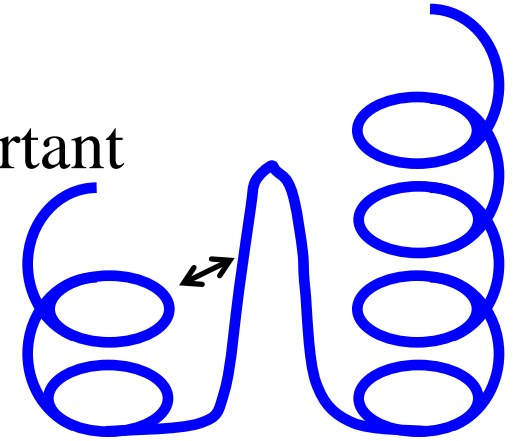
- will always favour unfolding

Debatable

- how much does entropy change with temperature ?
- depends on heat capacity of protein
- Two state model ? native  $\rightarrow$  denatured
  - what does  $\Delta G = 0$  mean ?
  - definitely too simple – proteins partially unfold

# proteins and systems

- energy
  - energy of native state is important but
  - energy of denatured state is equally important
- consequence
  - naïve optimisation may not work
  - you propose to make a protein more stable by putting in residues with opposite charge
    - lowers energy of native structure
    - also lowers energy of non-native structure



# proteins and systems

- you are always looking at  $\Delta G = G_{native} - G_{denatured}$
- nobody knows what the denatured state looks like


not just for temperature

- chemical denaturant ?
  - maybe simply binds to unfolded protein
    - lower energy – more stable

water is important (water entropy)

- unfolding a protein changes water order
- correct way to look at system is
$$\Delta G = G_{native\_protein+water} - G_{denatured\_protein+water}$$
- next ... motions in proteins

cannot be  
measured



# Motions, frequencies and proteins

Andrew Torda, Wintersemester 2009 / 2010, GST

- Motions and dynamics in proteins
  - how big are they ?
  - how fast are they ?
- Examples
- Types
  - without barriers
  - with barriers
- Energies
  - equal probability
  - not equal probability

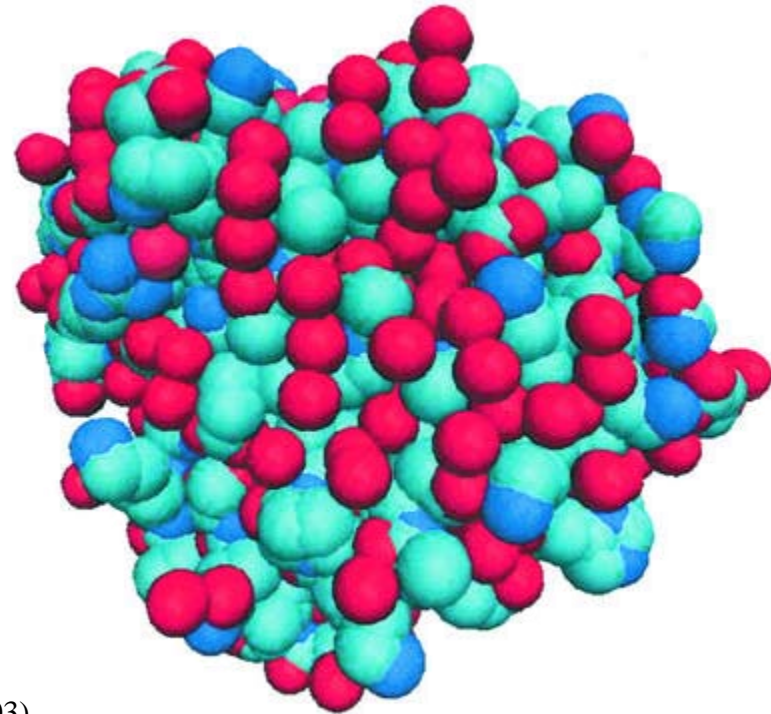
# Nasty question .. answered later

- I have motions in a protein at  $T=273$  (cold)
- heat protein to 300 K
  - do the frequencies of motions change ?



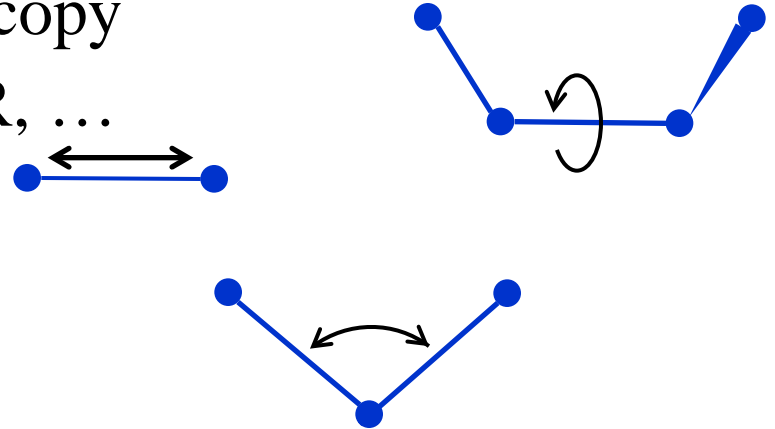
# Protein motion examples

- Early evidence that motions are important
  - myoglobin structure (1962)
    - carries  $O_2$ , maybe first protein structure solved
    - no channel could be found for  $O_2$  to reach haem group
    - could only be explained if parts of protein move and open up
- many similar stories
  - activity of protein cannot be explained by simple structure



# Protein motion examples

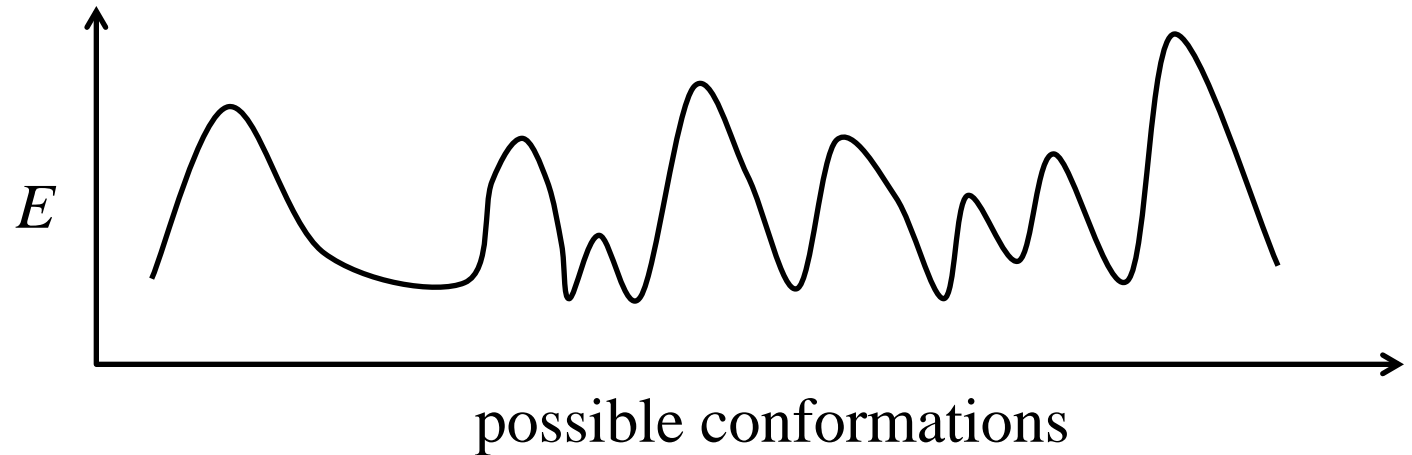
- Fundamental arguments
  - bonds, angles vibrate, rotate
  - basis of many kinds of spectroscopy
    - infra red, fluorescence, NMR, ...
- More fundamental arguments
  - at  $T = 0$  everything dead
  - at  $T = 300$  (this room) everything has kinetic energy
    - everything is moving
    - meaning of temperature ?  $T, E_{kin}$  ?
      - $\frac{1}{2} m v^2$



$E_{kin}$	kinetic energy
$T$	temperature

# Energy surfaces

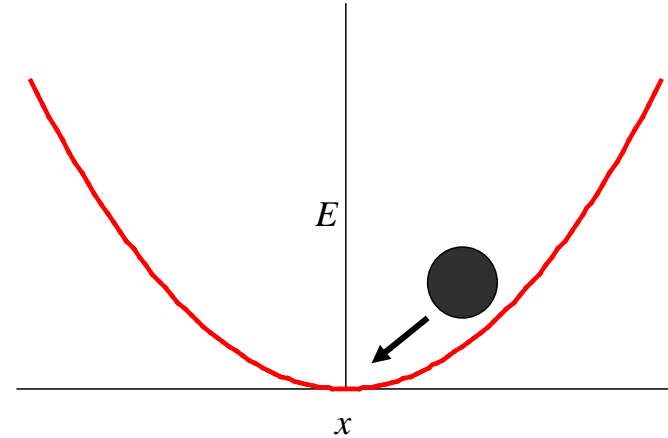
- run around on an energy surface



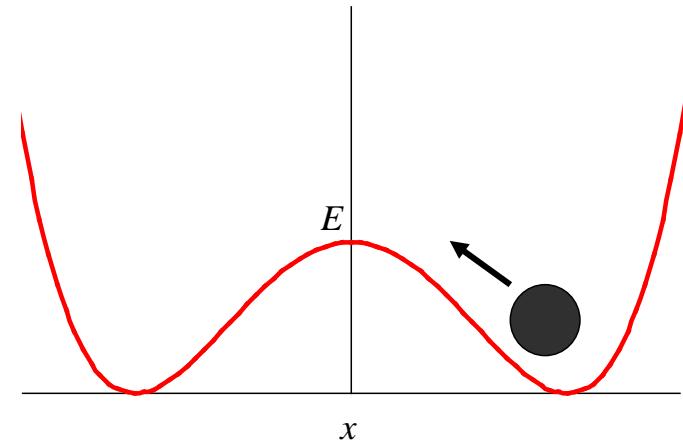
- energy surface and energy should determine motions
  - too complicated
  - energy surface not well known
- work with simpler models

# Motions with or without barriers

- Without barriers
  - one state + fluctuations



- With a barrier
  - two states

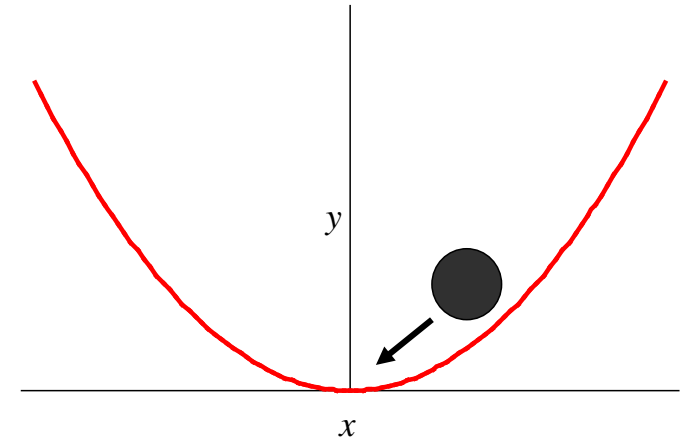


- both ideas simpler than previous picture

# Harmonic oscillators

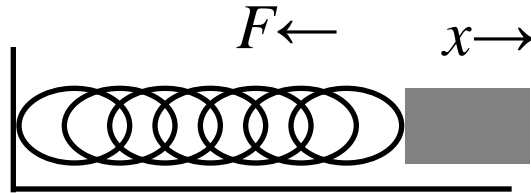
- find them everywhere..
  - energy =  $kx^2$
  - what is the frequency of motion  $\omega$  ?

$$x(t) = A \cos(\omega t + \delta)$$



- $A$  is the amplitude
- $\omega$  is the frequency
- $\delta$  is phase
- Detour .. why does this make sense

# Harmonic oscillator



$$F = -kx$$

$$ma = -kx$$

$$m\ddot{x} = -kx$$

$$m \frac{d^2 x}{dt^2} = -kx$$

$$m \frac{d^2 x}{dt^2} + kx = 0$$

$$\text{say } \omega^2 = k/m \quad \text{so } \omega = \left(k/m\right)^{1/2}$$

$$\frac{d^2 x}{dt^2} + \omega^2 x = 0$$

- has a solution..

$$x(t) = A \cos(\omega t + \delta)$$

**Is the solution valid ?**

$$x(t) = A \cos(\omega t + \delta)$$

$$\frac{dx}{dt} = A(-\sin(\omega t + \delta))\omega$$

$$= -A\omega \sin(\omega t + \delta)$$

$$\frac{d^2x}{dt^2} = -A\omega \cos(\omega t + \delta)\omega$$

$$= -A\omega^2 \cos(\omega t + \delta)$$

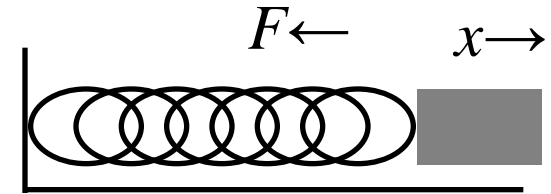
$$= -\omega^2 (A \cos(\omega t + \delta))$$

- which can be re-written as  $\frac{d^2x}{dt^2} = -\omega^2 x$

**Is the solution valid ?**

$$x(t) = A \cos(\omega t + \delta)$$

- from first arguments  $\frac{d^2 x}{dt^2} + \omega^2 x = 0$
- so  $-\omega^2 x + \omega^2 x = 0$
- and  $x(t) = A \cos(\omega t + \delta)$  is a solution
- back to  $\frac{d^2 x}{dt^2} = -\omega^2 x$

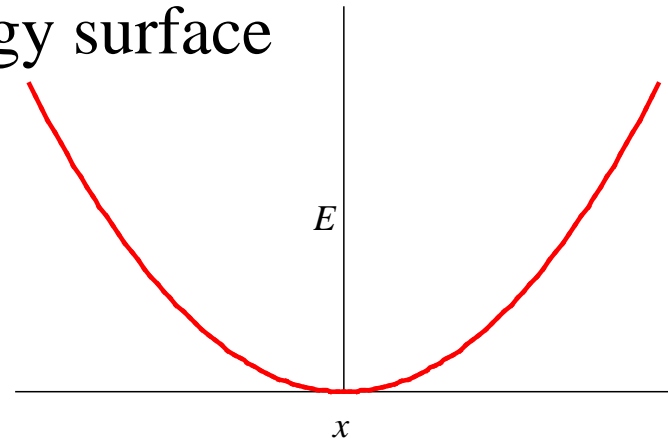




# Frequency and energy models

$$\frac{d^2x}{dt^2} = -\omega^2 x$$

- What is meaning of  $\frac{d^2x}{dt^2}$ 
  - second derivative / curvature
- What happens if you change temperature ?
  - angular frequency  $\omega$  depends on energy surface
  - temperature does not appear here
  - what does change ?



# Changing temperature (oscillator)

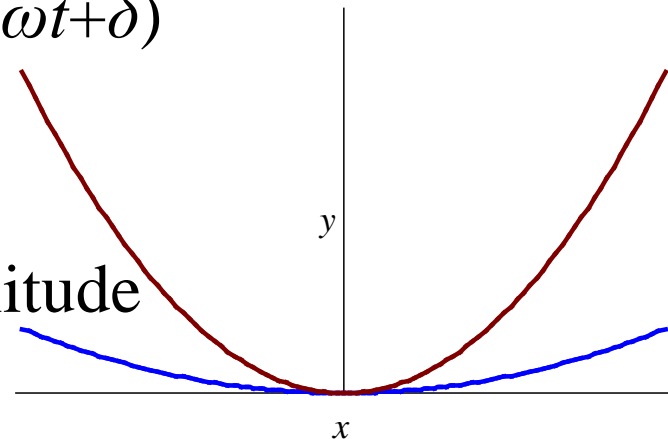
- Change temperature

- $E_{kin}$  changes
- $E_{kin} = \frac{1}{2} m v^2$
- $E_{kin} = \frac{1}{2} m A^2 \omega^2 \sin^2(\omega t + \delta)$
- amplitude changes

$$\frac{dx}{dt} = \dot{x} = v = -A \omega \sin(\omega t + \delta)$$

# Frequencies and amplitudes

- For a given temperature
  - energy distributes amongst modes/ degrees of freedom
  - $E_{kin}$  the same for different modes
  - $E_{kin} = \frac{1}{2} mv^2 = \frac{1}{2} mA^2\omega^2\sin^2(\omega t + \delta)$
- I have two modes in one protein
  - a slow motion / low frequency (bending of a hinge)
  - a fast / high frequency (movement of a sidechain)  
$$E_{kin} = \frac{1}{2} mv^2 = \frac{1}{2} mA^2\omega^2\sin^2(\omega t + \delta)$$
  - if  $\omega$  is low  $A$  is high
  - low frequency motions are large amplitude
  - big motions are slow

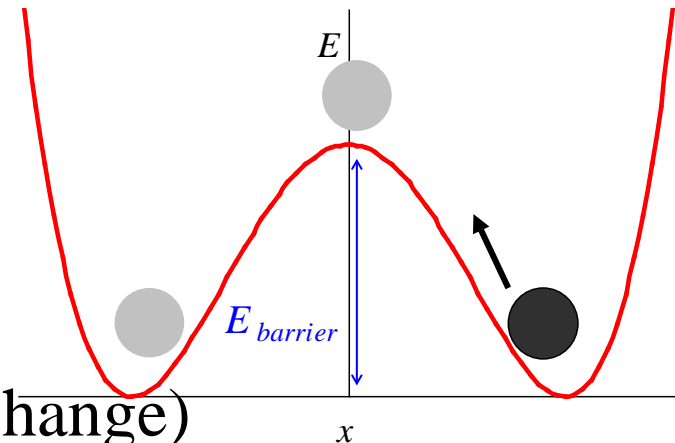
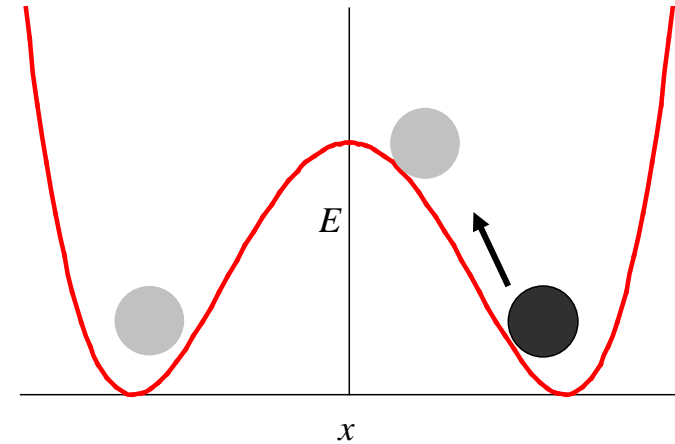


# Summary so far (harmonic oscillator)

- Maybe appropriate for motion without barriers
- only approximation
- frequencies do not depend on temperature
- we imagine a protein to have
  - many oscillators
  - some fast some slow
- bigger motions have lower frequency

# Movement with barriers

- how often do you move from right to left (and left to right)?
- our model
  - assume some random influences
  - velocity from  $E_{kin} = \frac{1}{2} mv^2$ ,  $v \propto E_{kin}^{1/2}$ 
    - better  $E_{kin}^{1/2}$  random
  - water molecules and other atoms are always hitting you
- if we reach the top
  - we may be moving slowly
    - may move to right (no change)
    - may fall into left energy well (change)
- consequence

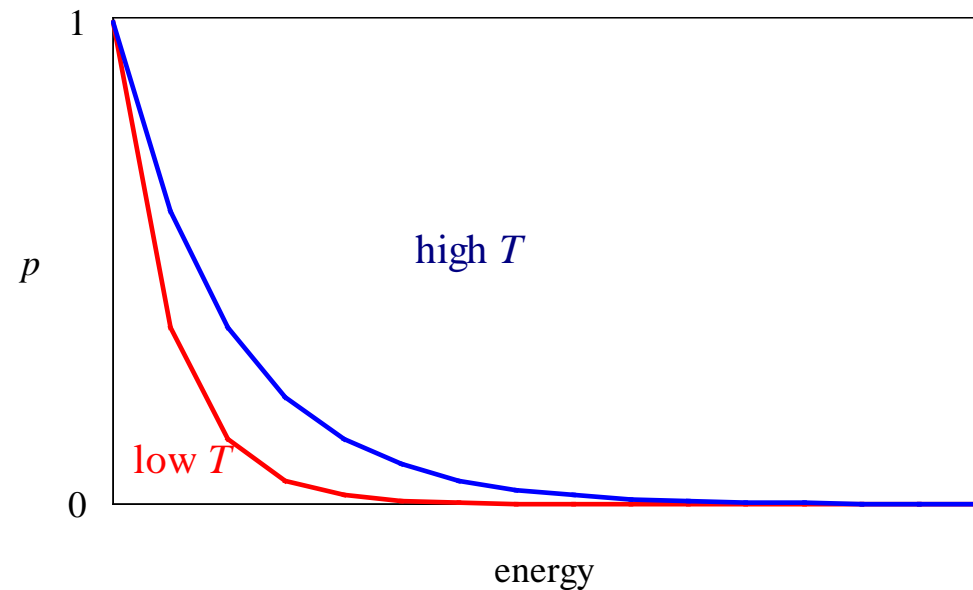


# Movement with barriers

- rate directly reflects
  - how often does a particle have enough energy to reach top of barrier ?
- Boltzmann rule... (more formal next semester)

$$p_i \propto e^{-E_i/kT}$$

- implications
  - small barriers (small  $E$ )
    - easy / fast to cross
  - as temperature  $\uparrow$  rate  $\uparrow$



$k$	Boltzmanns const
$T$	temperature

# Return to early question

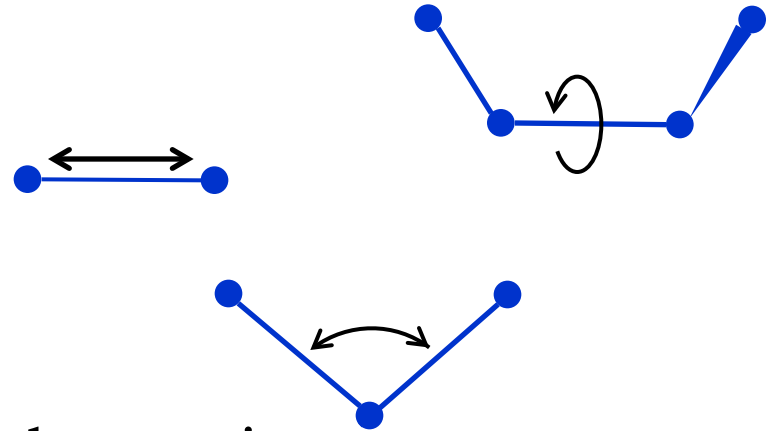
- do frequencies of motions change ?
  - if we have motion in a well (harmonic oscillator) .. No
  - if we move between energy minima ... Yes

## Which model is better ?

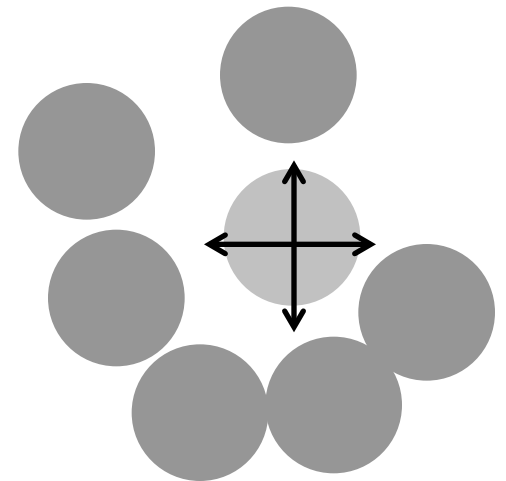
- empirical
  - raise temperature and see if it changes
- physical model
  - what you believe in..

# different kinds of motions (smaller)

- bond stretching, angle bending
  - nearly harmonic
- torsion angles
  - separate energy wells



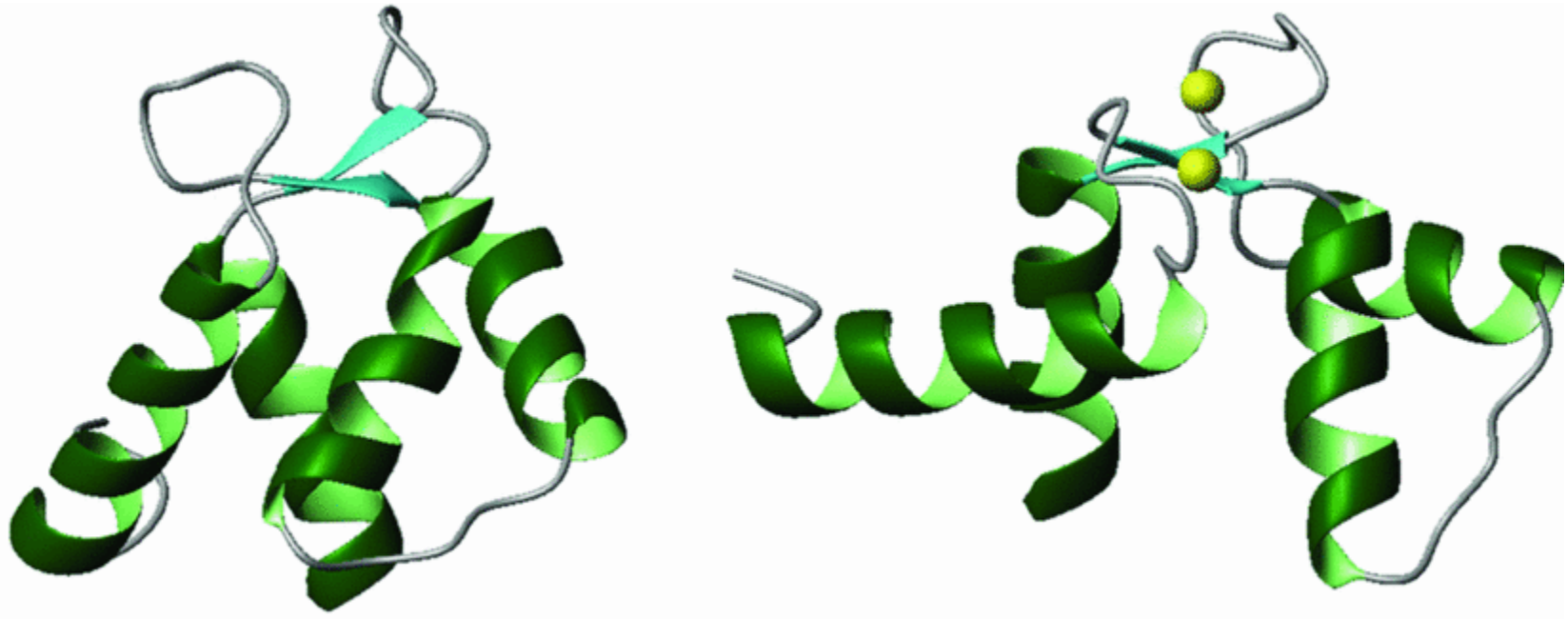
- other motions may be locally like harmonic
  - vibrations of packed atoms





# Bigger motions

- Calmodulin example
  - many Å and probably rather slow
  - too move from one conformation to the next – many barriers



# Summary

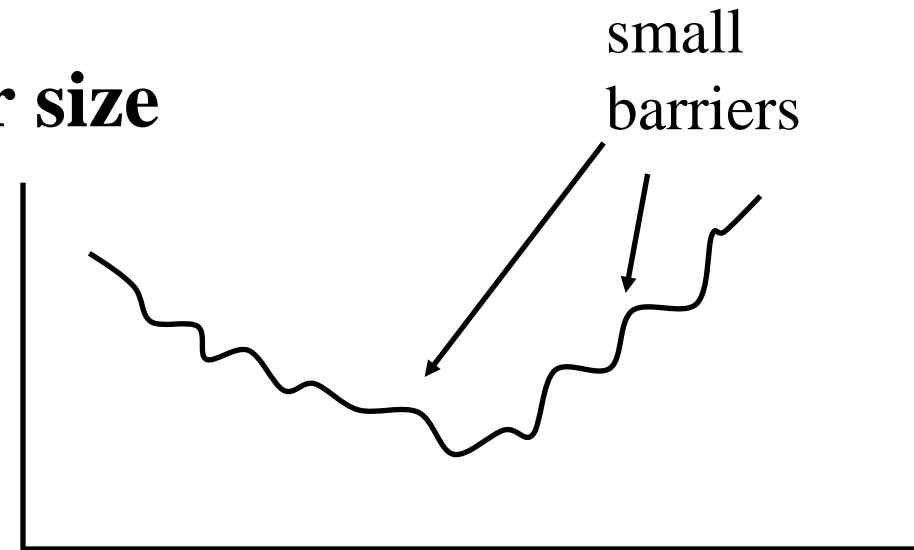
- models are too simple
  - most energy terms are not  $kx^2$ 
    - locally not a bad approximation
  - we do not have simple energy barriers
  - many more than two states
    - spectrum of motions
- many motions are a mixture (concerted)

# Detection of states

- Are all the different structures present at room temperature ?
- I have two states A and B
$$\frac{p_A}{p_B} = e^{\frac{E_A - E_B}{kT}}$$
  - if  $E_A - E_B$  much bigger than  $kT$  (some  $\text{kJmol}^{-1}$ )
    - only one state will be seen

## Barrier size

- Barriers very small
  - all particles have plenty of energy
  - effectively not present
- may be the case for some rotations



# Types of motions

motion	amplitude Å	$\log_{10}$ of time (s)
bond vibration	0.01 – 0.1	-14 to -13
sidechain rotation surface sidechains	5 – 10	-11 to -10
protein hinge bending	1 – 5	-11 to -7
sidechain rotation inside protein	5	-4 to 0
helix / strand breakage	5 – 10	-5 to 1

# Summary

- Motions are necessary to explain chemistry
- NMR and X-ray structures are time averages
- usually
  - small motions fast
  - big movements slow
- temperature dependence
  - different for different kinds of movement
  - can be used to estimate energy barriers