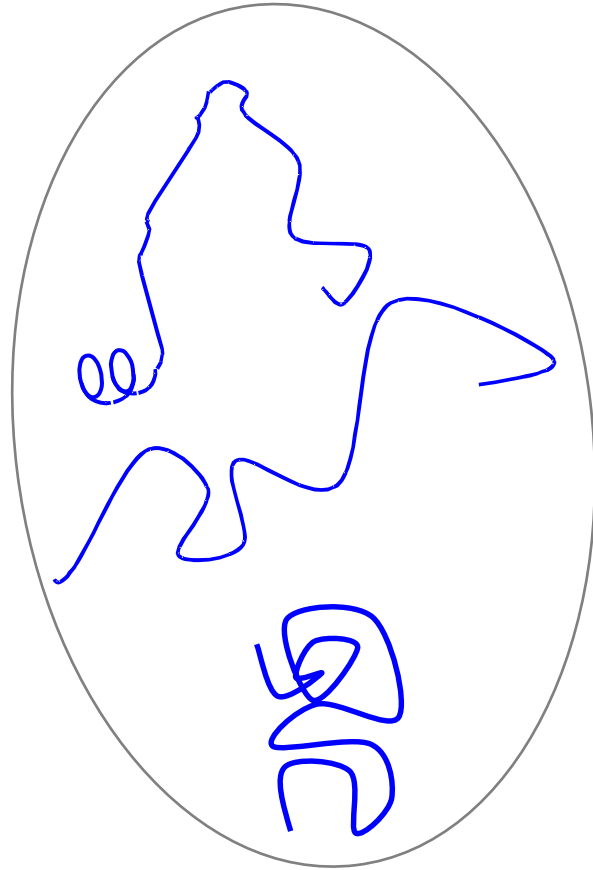


Protein stability

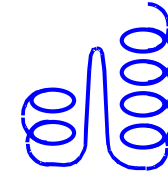
Our model

Andrew Torda, Wintersemester 2016 / 2017 GST



denatured (D)
unfolded
non-native

ΔG



native
(N) folded

Free energy change on

- folding
- denaturing ($-\Delta G$)

For a stable protein

$$\Delta G_{N \rightarrow D} > 0$$

Nomenclature – not for discussion

Make sure the following words are clear

- enthalpy
- free energy
- denatured / unfolded

Protein Stability

- what is known empirically
- definitions
- a stability surprise
- some explanations
- weaknesses of models

ΔG convention

$$\Delta G_{folding} = - \Delta G_{unfolding}$$

Define $\Delta G > 0$ as stable so reaction is

folded \rightarrow unfolded

(native \rightarrow denatured)

more positive ΔG , more stable the protein

Empiricism / rules

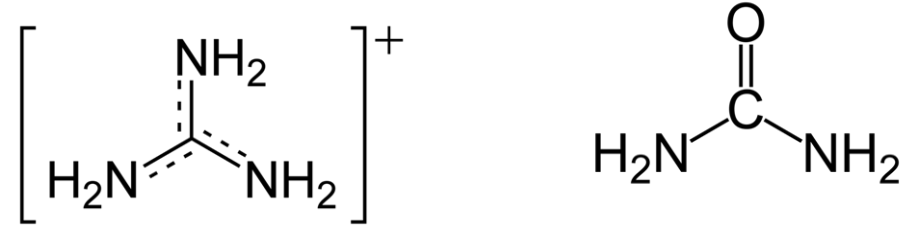
- most proteins are marginally stable ($\Delta G \approx 0$)
- proteins can be denatured by
 - pH, ions, temperature, solvent, surface area, urea (example later)
- too hot ?
 - eggs cook, people die
- big variation
 - some bacteria live at 373 K – their proteins are not denatured

Explain denaturing

Why do these denature a protein ?

pH, concentrated ions, temperature, solvent, surface area

- pH ? change the charge on some groups, remove favourable interactions
- ions ? provide competition for charges, H-bonds



- temperature ? add kinetic energy, push particles out of minima
- solvent ? remove favourable protein-solvent interactions
- surface area ? surface tension / protein – air interactions

Rules

Nature cares about free energy ΔG we measure free energy, not potential energy

$$\Delta G = \Delta H - T\Delta S$$

- G free energy (Gibbs)
- H enthalpy
potential energy including volume effects $U + PV$
- S entropy

Formula will come back – remember

- two contributions
 1. entropy always favours unfolding
 2. enthalpy / potential energy will favour folding

Measurement

Folded / Unfolded

- how to measure
 - spectroscopy
 - absorbance (optical / UV spectroscopy)
 - rotational (CD / ORD)
 - fluorescence
 - NMR
 - activity
 - ...
- usually – two states (native / denatured) that somehow look different

Energies

- calorimetry
- measurements of [native] / [denatured]

Experimental - measure ΔG ?

How do I measure ΔG for a reaction $A + B \rightarrow C$?

- calorimetry ? measure the heat released
 - for a protein, reaction is folded \rightarrow unfolded
 - Could one prepare protein and watch it fold ? Difficult

Alternative view – for any reaction $A \rightarrow B$ at equilibrium

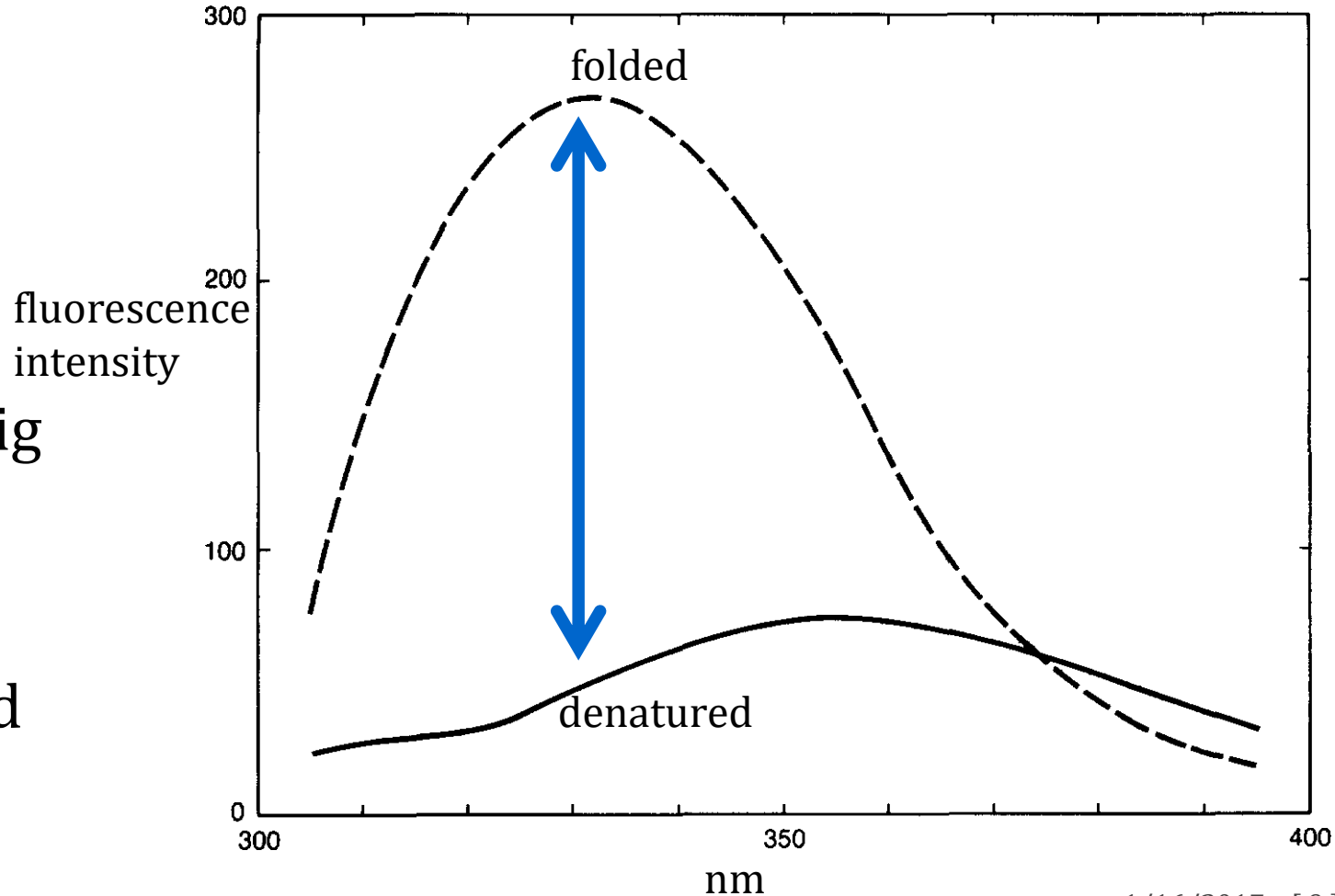
- $\Delta G = RT \ln \frac{[B]}{[A]}$ or in our case $\Delta G = RT \ln \frac{[\text{unfolded}]}{[\text{folded}]}$

Problem

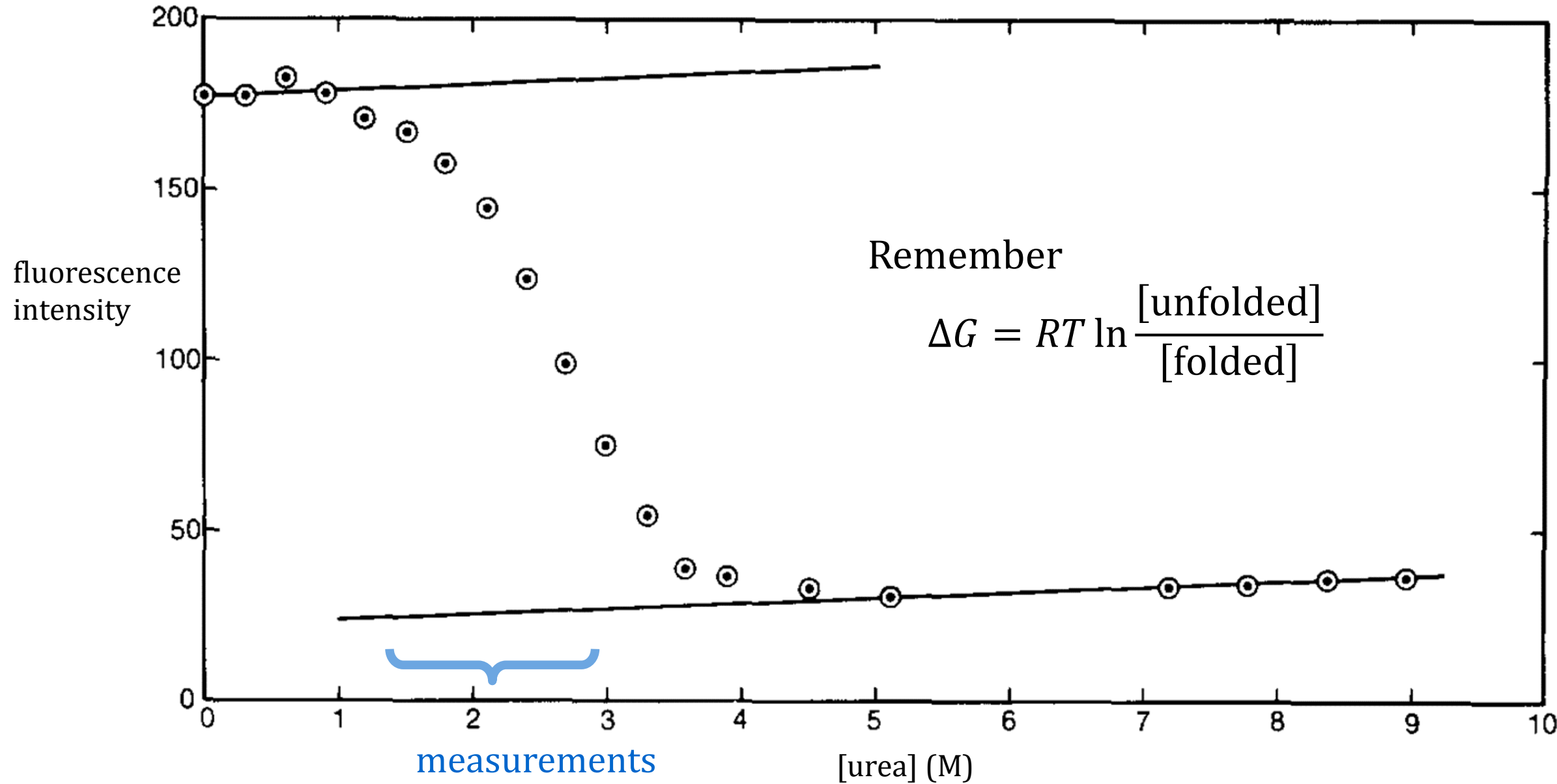
- under normal conditions $[\text{unfolded}]$ is too small
- if $\frac{[\text{unfolded}]}{[\text{folded}]} = 10^{-4}$ or 10^{-5} could you see it ?

Assume

- you have some kind of spectroscopy (CD, fluorescence, ...)
- you can detect a signal for folded and unfolded
- if the protein is partially folded
you can estimate ΔG
- if $\frac{[\text{unfolded}]}{[\text{folded}]}$ is not too small or big
I can measure it
- trick is to make it partially unfold

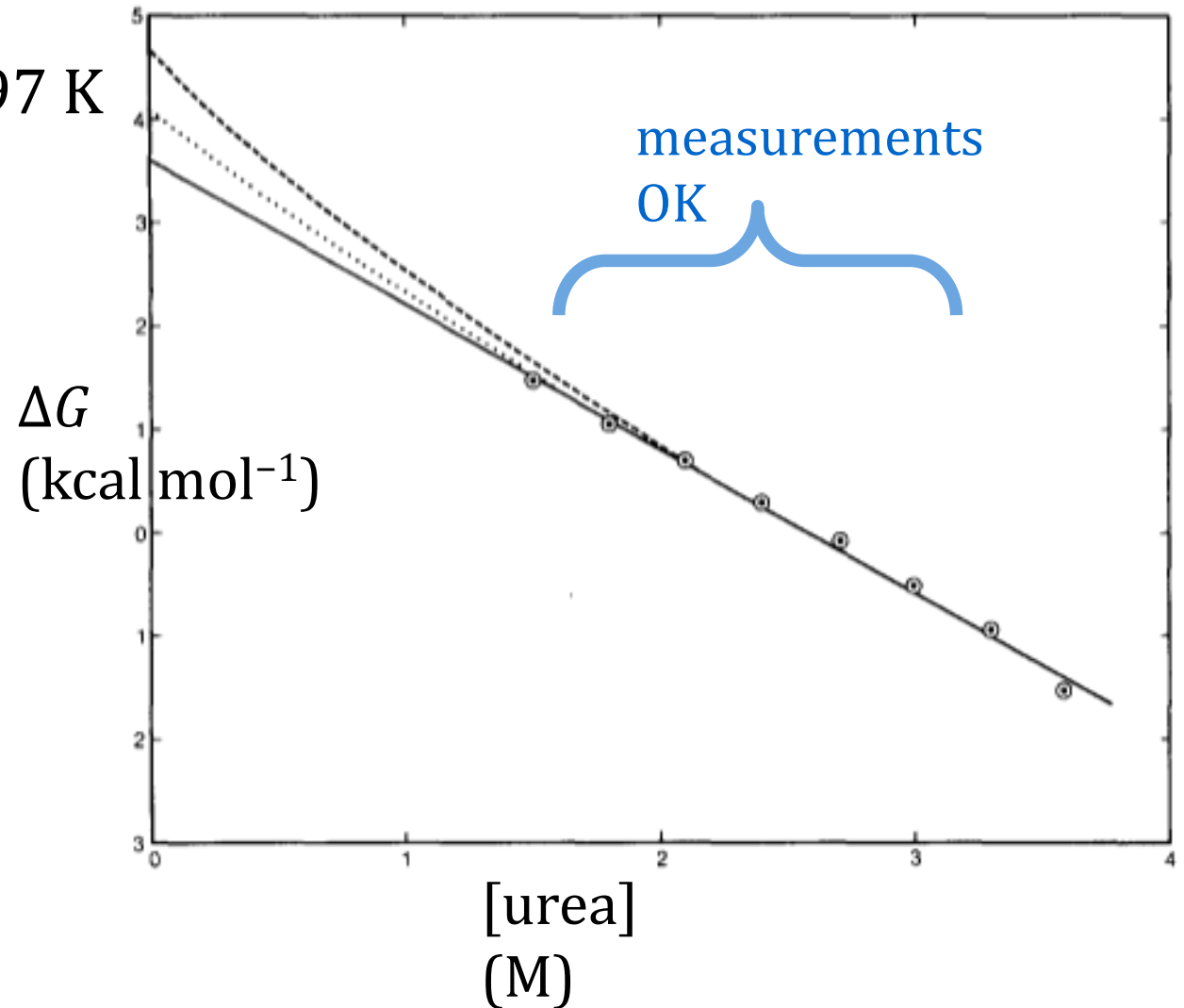


Add denaturant



Experimental - measure ΔG ?

- From spectroscopy, estimate ΔG for each temperature / [urea]
- Extrapolate back to zero urea or 297 K
- Far from perfect - do not ask me if the line is really a line

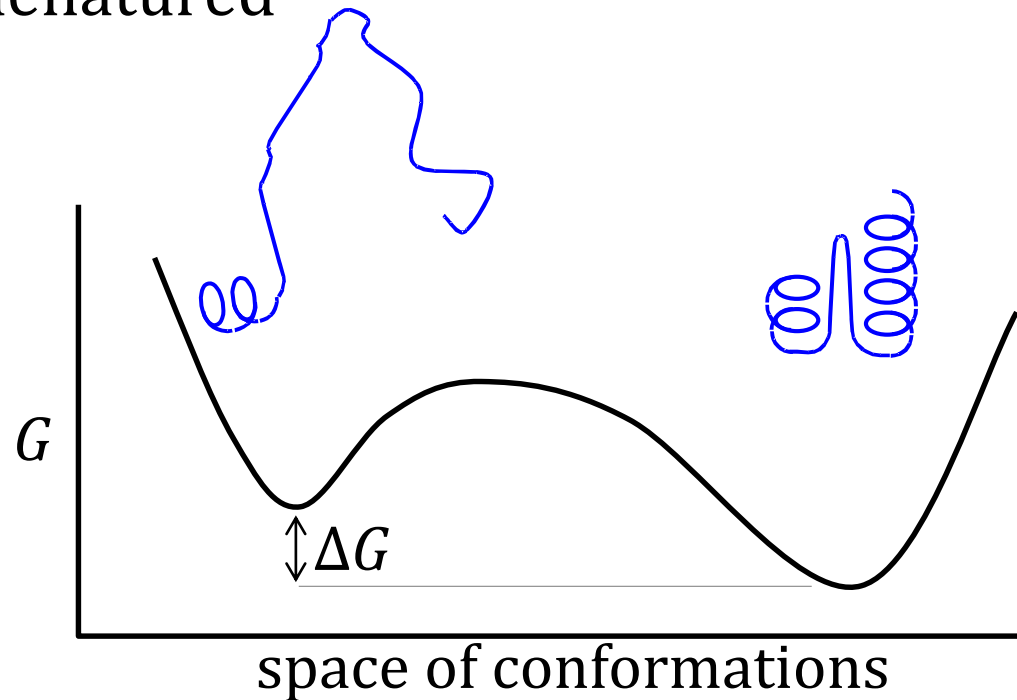


Two state model

Model requires an energy barrier

What if $\Delta G = 0$?

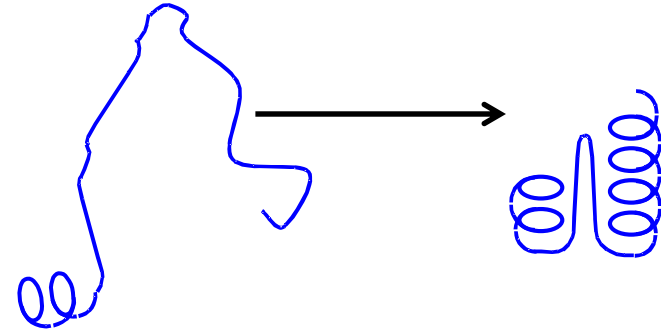
- $\frac{1}{2}$ molecules folded
- $\frac{1}{2}$ molecules denatured



First picture of stability

What holds a protein together ?

- forces between atoms
 - bonds, electrostatic, Lennard-Jones
- atoms also repel



Cannot be so simple

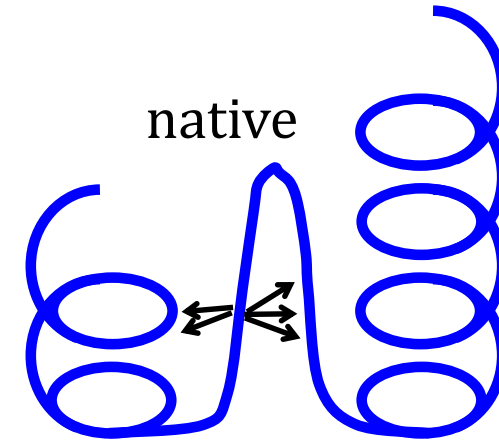
- atoms would just fall into correct position
- ΔG would always be very positive
- missing ?
 - effect of solvent
- in native structure there are "correct contacts"

Balance of energy terms

Refer to contacts in native structure as correct

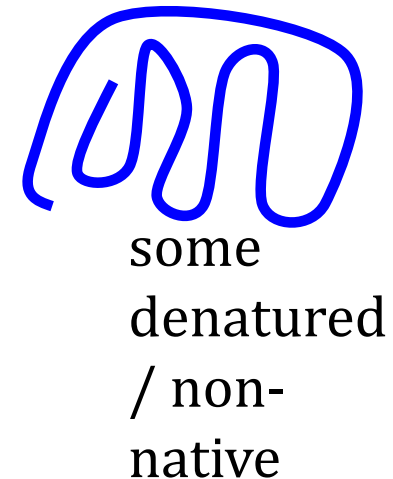
One atom in native structure

- interacts with correct neighbours



In the non-native structures there are also contacts

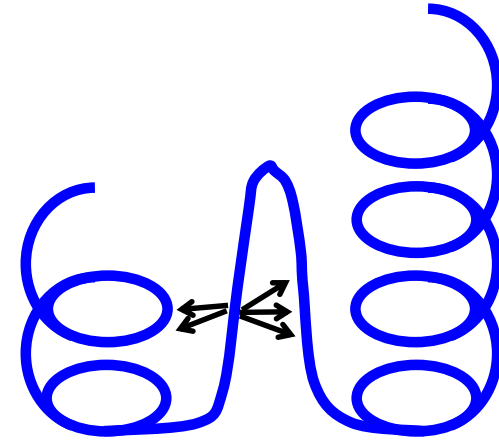
- atom interacts with “wrong” neighbours
- balance of forces
- stability has to do with
 - energy / enthalpy $H_{\text{native}} - H_{\text{denatured}}$



Balance of energy terms

More forces

- how many polar / charged groups are there ?
 - NH + CO backbone every residue
 - polar / charged sidechains
- all can interact with water



- stability will also depend on

$$H_{native_water} - H_{unfolded_water}$$

Balance of energies

(Klausur Frage)

- contacts in native structure
- contacts in unfolded structure
- contacts of native protein with water
- contacts of unfolded protein with water

Entropy version 1

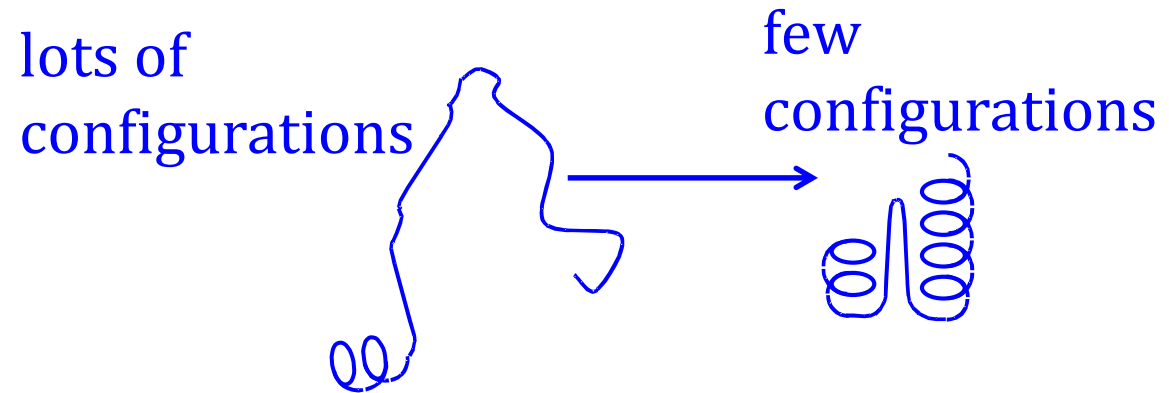
$$\Delta G = \Delta H - T \Delta S$$

- considered ΔH terms, what is $\Delta S_{folded \rightarrow unfolded}$?
 - entropy depends on the number of conformations ($k \ln \Omega$) or better

$$S = -k \sum_{i=1}^{N_{states}} p_i \ln p_i$$

As a protein unfolds

- number of conformations \uparrow
- entropy goes \uparrow
- entropy / ΔS will favour denaturing

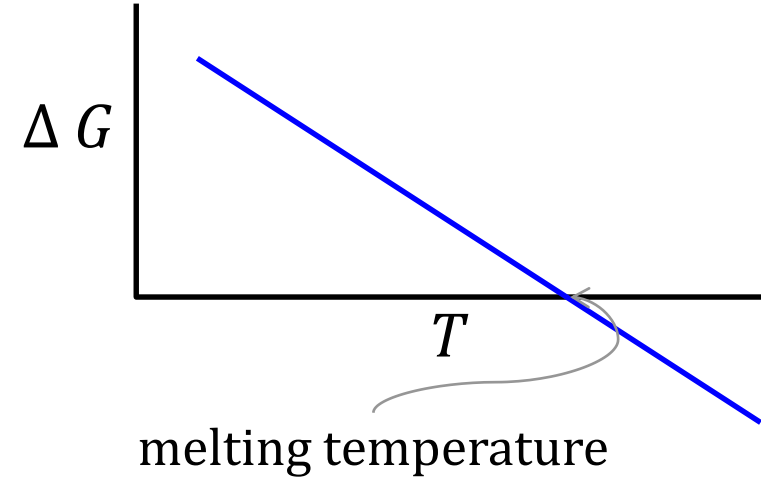
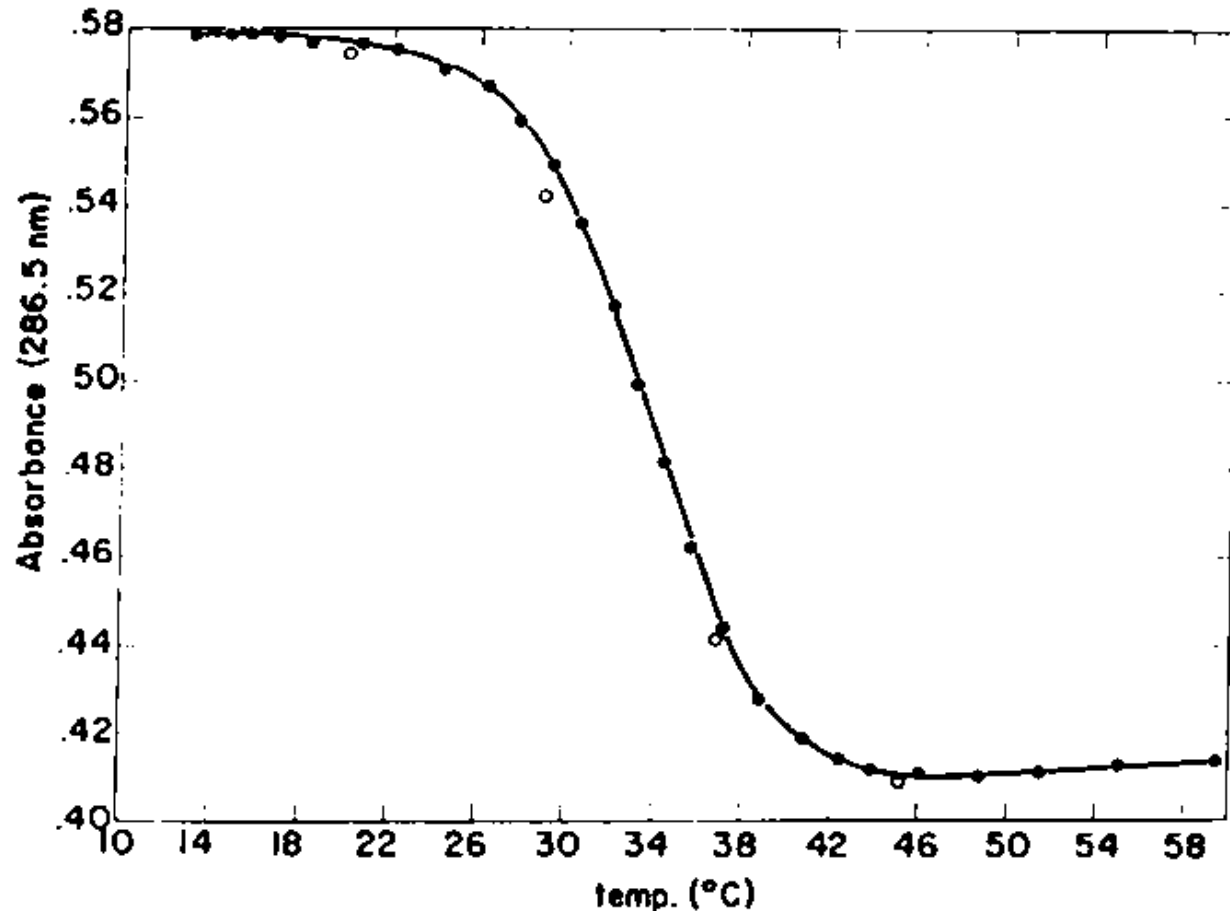


Ω_x number of states in x
 k Boltzman constant

Balance of forces version 1

$$\Delta G = \Delta H - T \Delta S$$

- proteins should melt / cook / fall apart if you heat them



ribonuclease unfolding

Entropy version 2

$$\Delta G = \Delta H - T \Delta S$$

- is ΔS a constant? Is it T dependent?
- meaning of $\Delta S_{folded-unfolded}$
- roughly how does the number of states change?

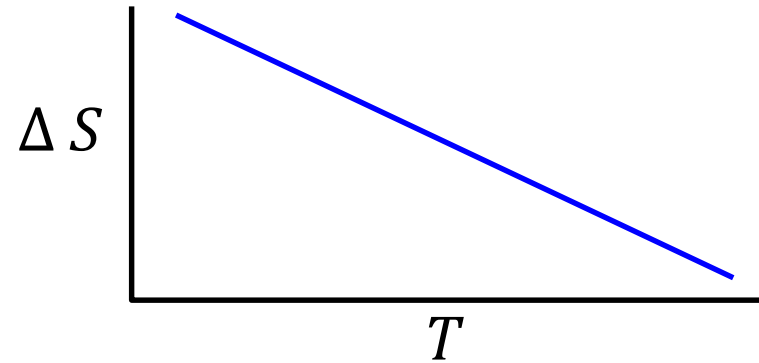
$$\begin{aligned}\Delta S &= S_{folded} - S_{unfolded} \\ &= k(\ln \Omega_{folded} - \ln \Omega_{unfolded}) \\ &= k \ln \frac{\Omega_{folded}}{\Omega_{unfolded}}\end{aligned}$$

- Ω_{folded} definitely goes up with temperature

Ω_x number of states in x

Entropy change on unfolding

One has a curve like



Radical consequence

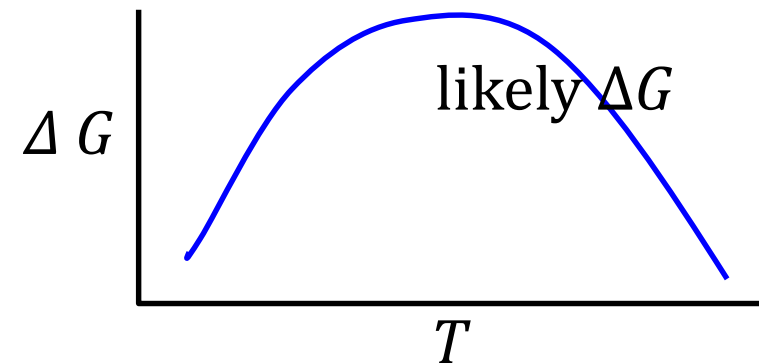
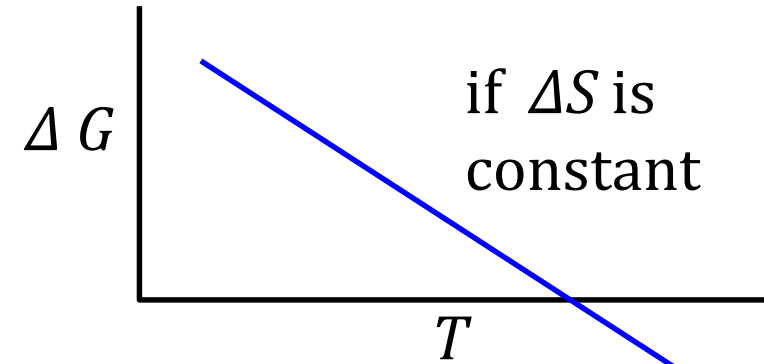
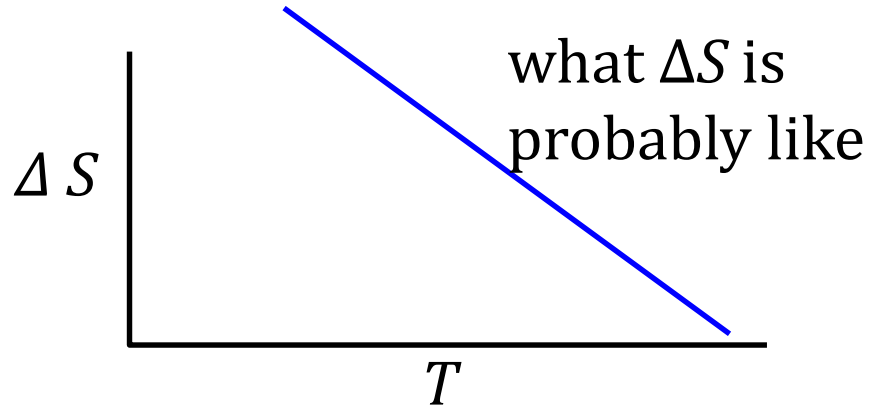
- entropy might make proteins less stable as you cool them

Can one cook an egg by cooling it ?

Combining these properties

protein stability

$$\Delta G = \Delta H - T \Delta S$$

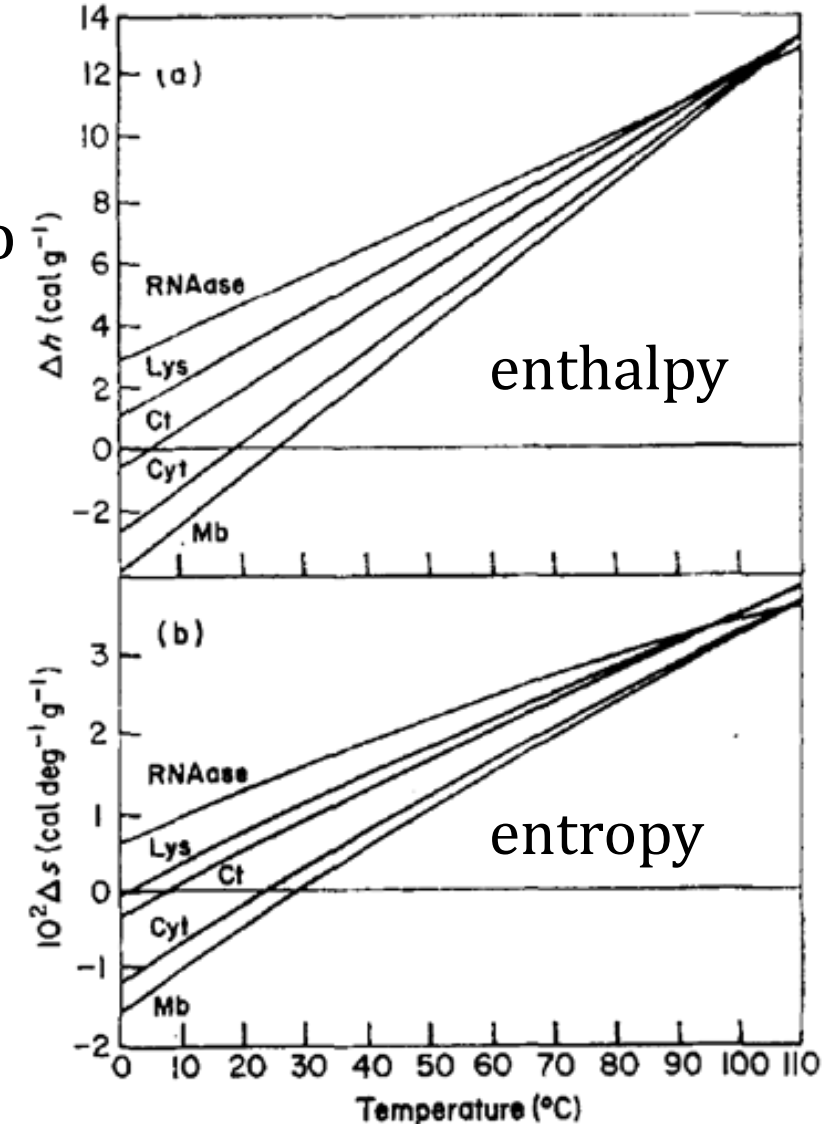


What is seen / claimed ?

Old measurements

- protein stability (ΔG) is a balance of energy and entropy
- note sign convention
$$\Delta G = \Delta H - T \Delta S$$
- difference of two large numbers comes to nearly zero
- what might you expect ?

lysozyme
RNAase
chymotrypsin
myoglobin
cytochrome C



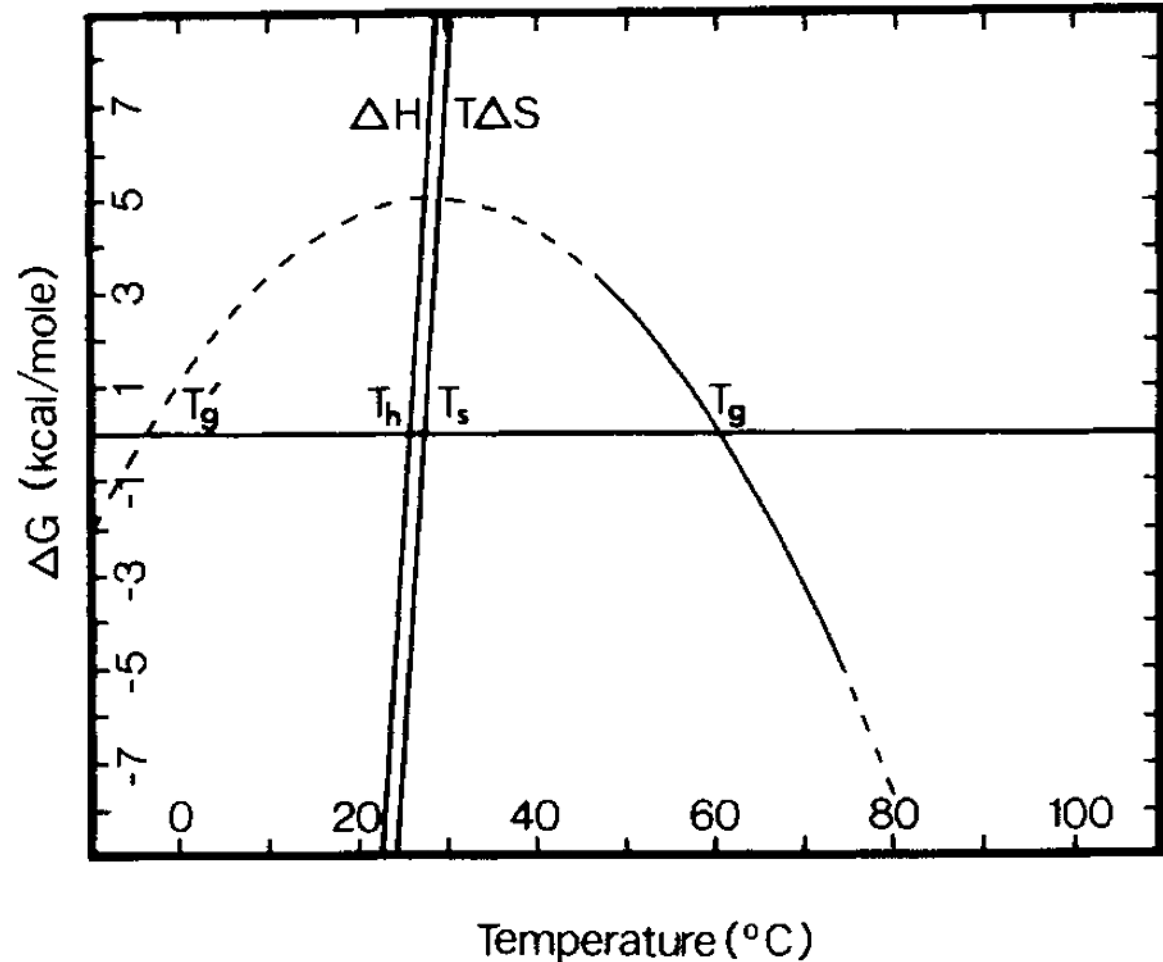
final version

Claim.. for typical protein

- bold line –measured
- dashed – extrapolated

Implies

- you can denature a protein by cooling (cook egg by freezing ?)
- what is measured ?



free energy experimental

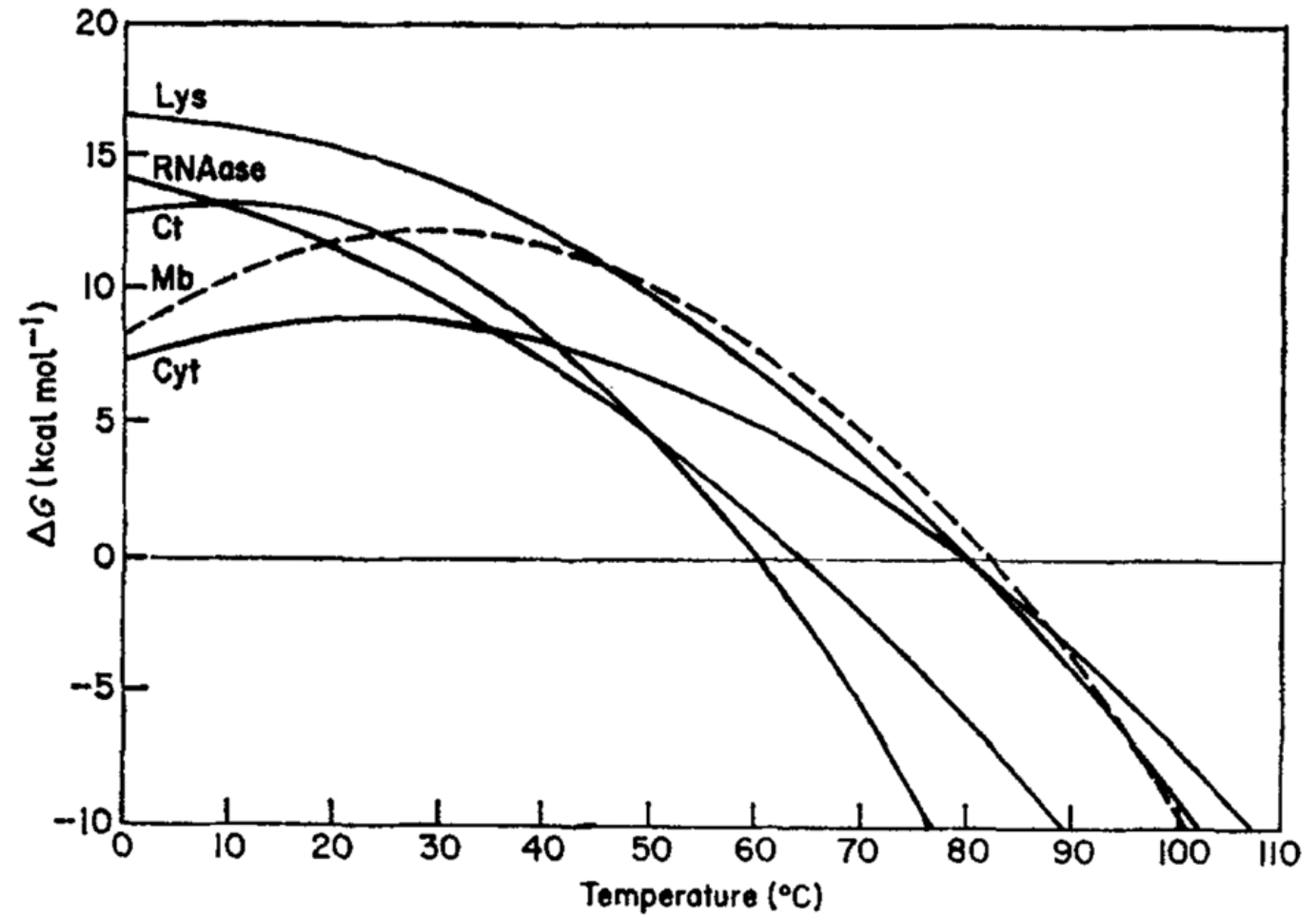
Looks like there will be cold denaturing

- below zero

Curve is different for all proteins

Does this prove "cold denaturing" ?

lysozyme
RNAase
chymotrypsin
myoglobin
cytochrome C



Cold denaturing

Controversial

Often predicted to happen below 0°

- hard to measure

Entropy and Enthalpy Summary / Consequences

Enthalpy H / potential energy

- will always favour folding

Entropy

- will always favour unfolding

Debatable

- how much does entropy change with temperature ?
- Two state model ? native \rightarrow denatured
 - what does $\Delta G = 0$ mean ?
 - definitely too simple – proteins partially unfold

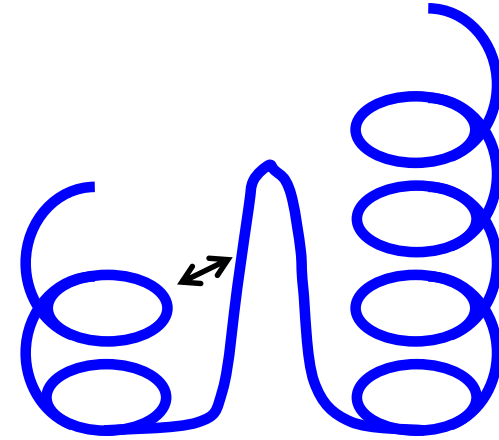
proteins and systems

Energy

- energy of native state is important but
- energy of denatured state is equally important

Consequence

- naïve optimisation may not work
- you propose to make a protein more stable by putting in residues with opposite charge
 - lowers energy of native structure
 - also lowers energy of non-native structure



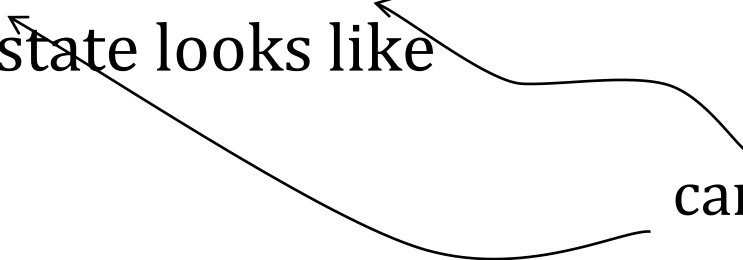
proteins and systems

- you are always looking at $\Delta G = G_{native} - G_{denatured}$
- nobody knows what the denatured state looks like

Not just for temperature

- chemical denaturant ?
 - maybe simply binds to unfolded protein
 - lower energy – more stable

cannot be
measured



Water is important (water entropy)

- unfolding a protein changes water order
- correct way to look at system is
$$\Delta G = G_{native_protein+water} - G_{denatured_protein+water}$$
- next ... motions in proteins

Motions, frequencies and proteins

Motions and dynamics in proteins

- how big are they ?
- how fast are they ?

- Examples

Types

- without barriers
- with barriers

Energies

- equal probability
- not equal probability

Nasty question .. answered later

I have motions in a protein at $T=273$ (cold)

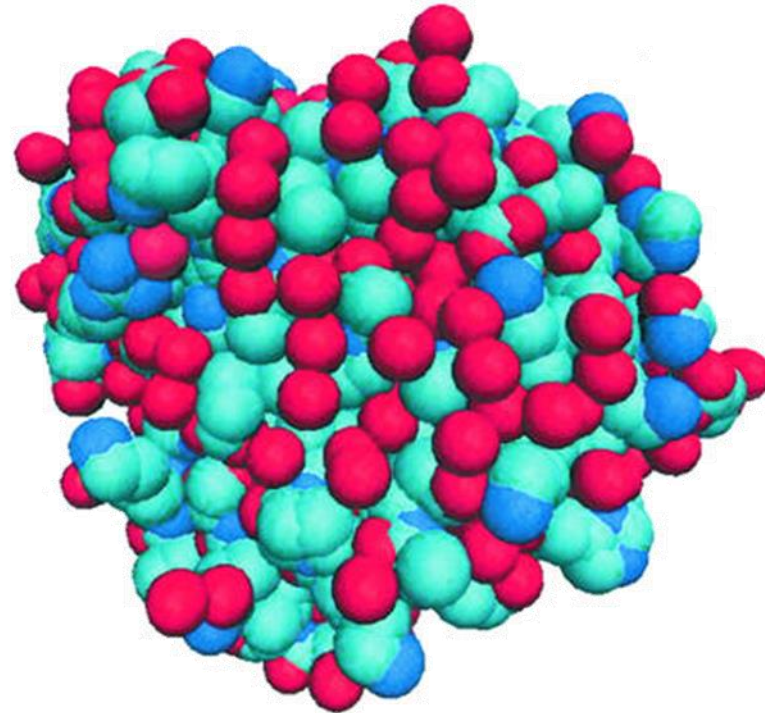
Heat protein to 300 K

- do the frequencies of motions change ?

Protein motion examples

Early evidence that motions are important

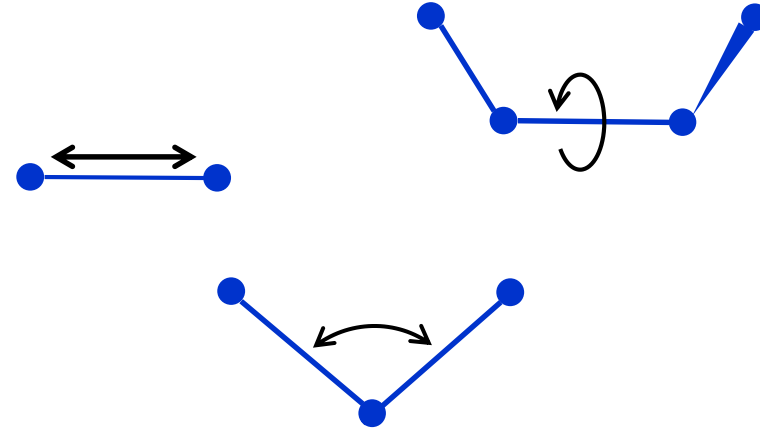
- myoglobin structure (1962)
 - carries O_2 , maybe first protein structure solved
- no channel could be found for O_2 to reach haem group
- could only be explained if parts of protein move and open up
- many similar stories
- activity of protein cannot be explained by simple structure



Protein motion examples

Fundamental arguments

- bonds, angles vibrate, rotate
- basis of many kinds of spectroscopy
 - infra red, fluorescence, NMR, ...



More fundamental arguments

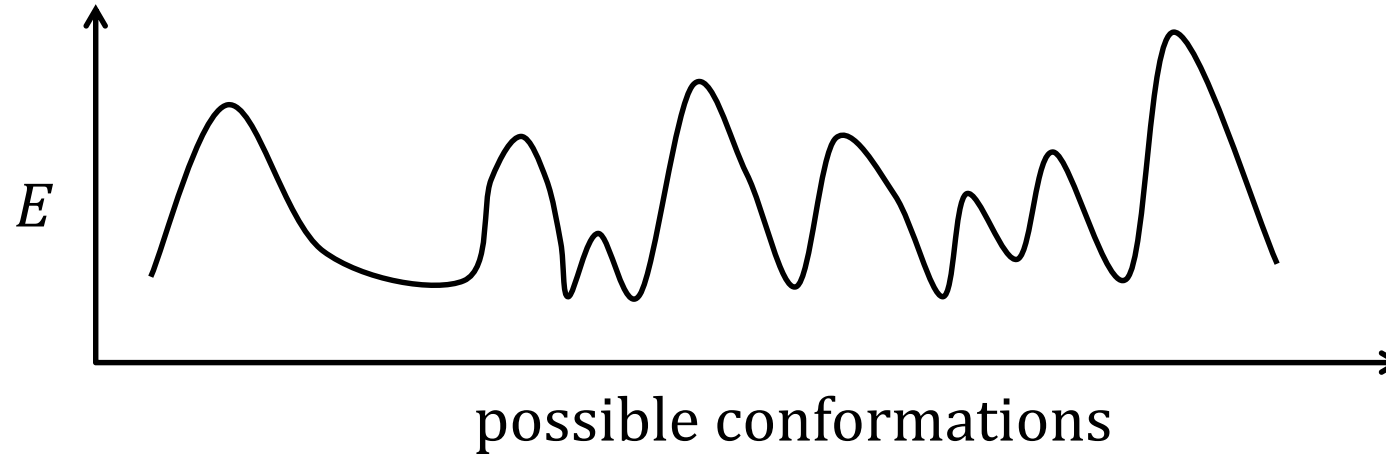
- at $T = 0$ everything dead
- at $T = 300$ (this room) everything has kinetic energy
 - everything is moving
 - meaning of temperature ? T, E_{kin} ?

$$\frac{1}{2}mv^2$$

E_{kin}	kinetic energy
T	temperature

Energy surfaces

Run around on an energy surface



Energy surface and energy should determine motions

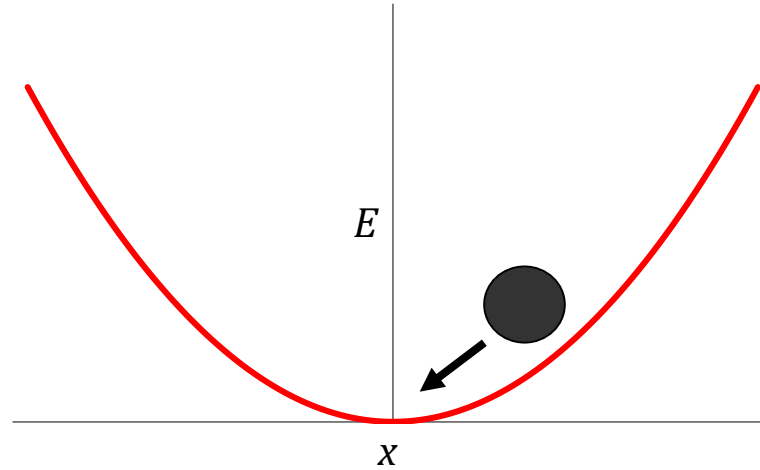
- too complicated
- energy surface not well known

Work with simpler models

Motions with or without barriers

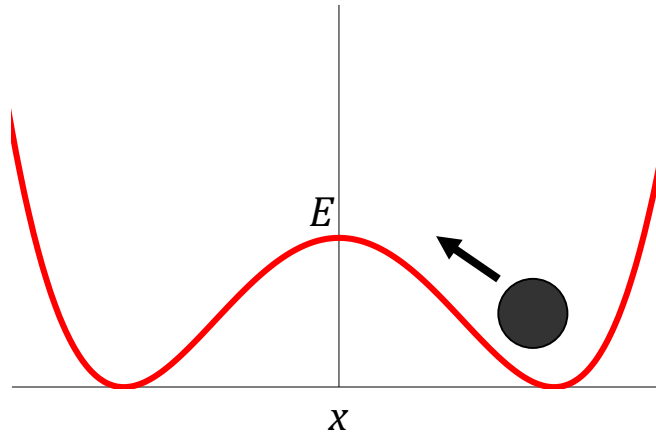
Without barriers

- one state + fluctuations



With a barrier

- two states



Harmonic oscillators

Find them everywhere..

- potential energy = kx^2
- what is the frequency of motion ω ?

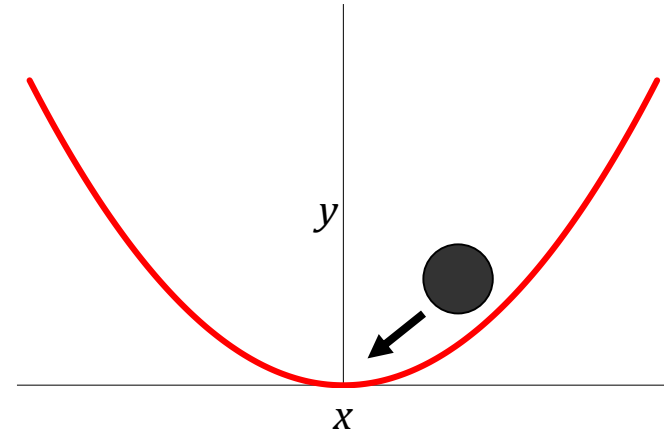
$$x(t) = A \cos(\omega t + \delta)$$

A is the amplitude

ω is the frequency

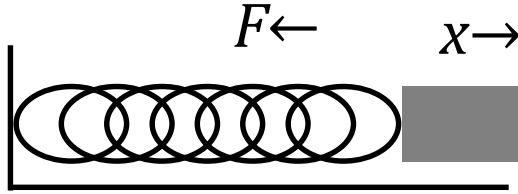
δ is phase

Detour .. why does this make sense ?



Harmonic oscillator

$$m \frac{d^2 x}{dt^2} + kx = 0$$



$$F = -kx$$

$$ma = -kx$$

$$\text{say } \omega^2 = \frac{k}{m} \text{ so } \omega = \left(\frac{k}{m}\right)^{1/2}$$

$$m \frac{d^2 x}{dt^2} = -kx$$

$$\frac{d^2 x}{dt^2} + \omega^2 x = 0$$

has a solution.. $x(t) = A \cos(\omega t + \delta)$

- can I convince you ?

Is the solution valid ? $x(t) = A \cos(\omega t + \delta)$

$$\begin{aligned}\frac{dx}{dt} &= A(-\sin(\omega t + \delta))\omega \\ &= -A\omega \sin(\omega t + \delta)\end{aligned}$$

$$\begin{aligned}\frac{d^2x}{dt^2} &= -A\omega \cos(\omega t + \delta)\omega \\ &= -A\omega^2 \cos(\omega t + \delta) \\ &= -\omega^2(A \cos(\omega t + \delta))\end{aligned}$$

which can be re-written as $\frac{d^2x}{dt^2} = -\omega^2 x$

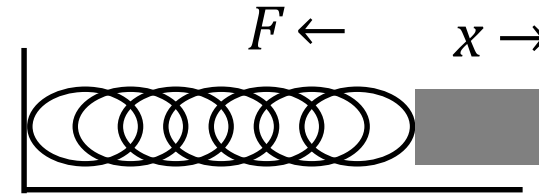
Is the solution valid ? $x(t) = A \cos(\omega t + \delta)$

From first arguments $\frac{d^2x}{dt^2} + \omega^2 x = 0$

$$-\omega^2 x + \omega^2 x = 0$$

so $x(t) = A \cos(\omega t + \delta)$ is a solution

and back to $\frac{d^2x}{dt^2} = -\omega^2 x$



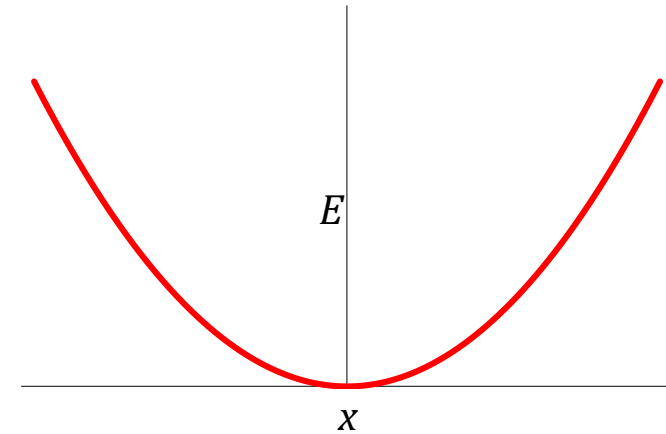
Frequency and energy models $\frac{d^2x}{dt^2} = -\omega^2 x$

What is meaning of $\frac{d^2x}{dt^2}$?

- second derivative / curvature

What happens if you change temperature ?

- angular frequency ω depends on energy surface
- temperature does not appear here
- what does change ?



Changing temperature (oscillator)

Change temperature

- E_{kin} changes
- $E_{kin} = \frac{1}{2}mv^2$
- $E_{kin} = \frac{1}{2}mA^2\omega^2 \sin^2(\omega t + \delta)$
- amplitude changes

$$\frac{dx}{dt} = \dot{x} = v = -A\omega \sin(\omega t + \delta)$$

Frequencies and amplitudes

For a given temperature

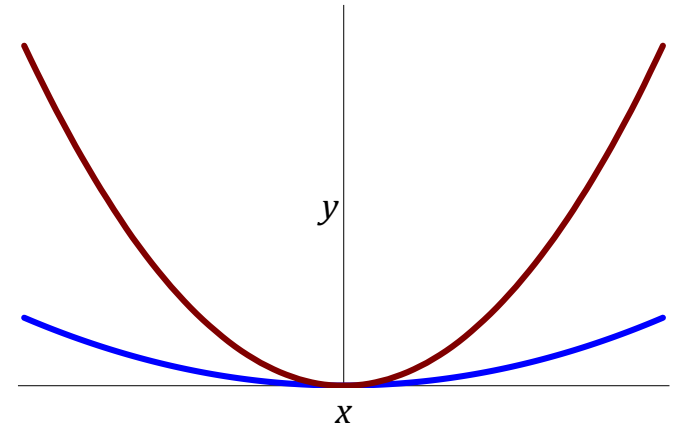
- energy distributes amongst modes/ degrees of freedom
- E_{kin} the same for different modes
- $E_{kin} = \frac{1}{2} m v^2 = \frac{1}{2} m A^2 \omega^2 \sin^2(\omega t + \delta)$

I have two modes in one protein

- a slow motion / low frequency (bending of a hinge)
- a fast / high frequency (movement of a sidechain)

$$E_{kin} = \frac{1}{2} m v^2 = \frac{1}{2} m A^2 \omega^2 \sin^2(\omega t + \delta)$$

- if ω is low, A is high
- low frequency motions are large amplitude
- big motions are slow



Summary so far (harmonic oscillator)

- Maybe appropriate for motion without barriers
- only approximation
- frequencies do not depend on temperature
- we imagine a protein to have
 - many oscillators
 - some fast some slow
- bigger motions have lower frequency

Movement with barriers

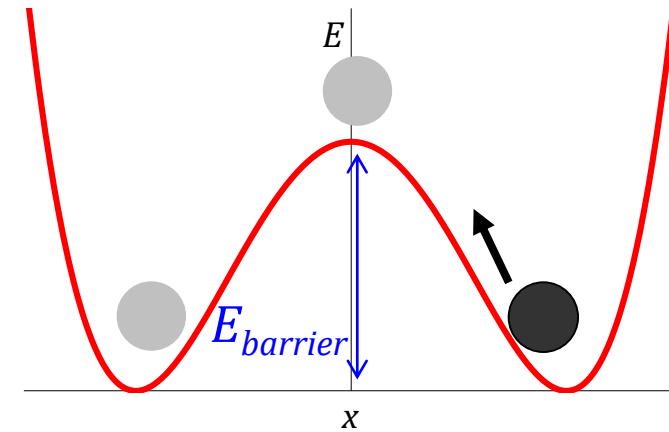
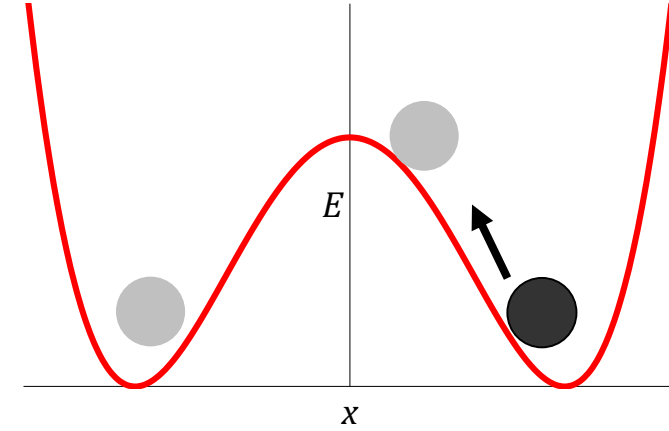
How often do you move right to left
(and left to right) ?

Our model

- assume some random influences
water and other atoms always hitting you
- velocity from $E_{kin} = \frac{1}{2}mv^2$, $v \propto E_{kin}^{1/2}$
 - better... $E_{kin}^{1/2} \pm \text{random}$

If we reach the top

- we may be moving slowly
 - may move to right (no change)
 - may fall into left energy well (change)
- consequence



Movement with barriers

Rate directly reflects

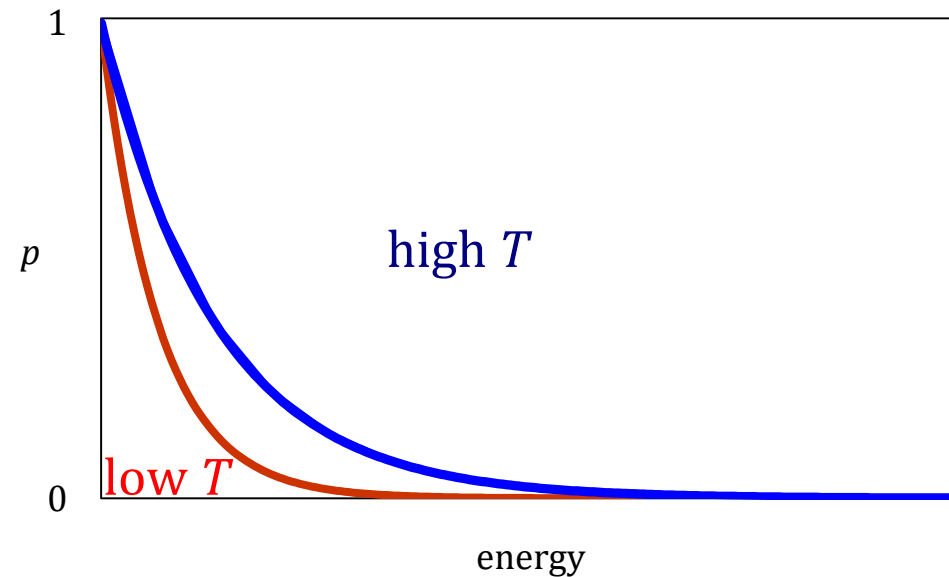
- how often does a particle have enough energy to reach top of barrier ?

Boltzmann rule... (more formal next semester)

$$p_i \propto e^{\frac{-E_i}{kT}}$$

Implications

- small barriers (small E)
 - easy / fast to cross
- as temperature \uparrow rate \uparrow



k	Boltzmanns const
T	temperature

Return to original question

Do frequencies of motions change ?

- if we have motion in a well (harmonic oscillator) .. No
- if we move between energy minima ... Yes

Which model is better ?

Empirical

- raise temperature and see if it changes

Physical model

- what you believe in..

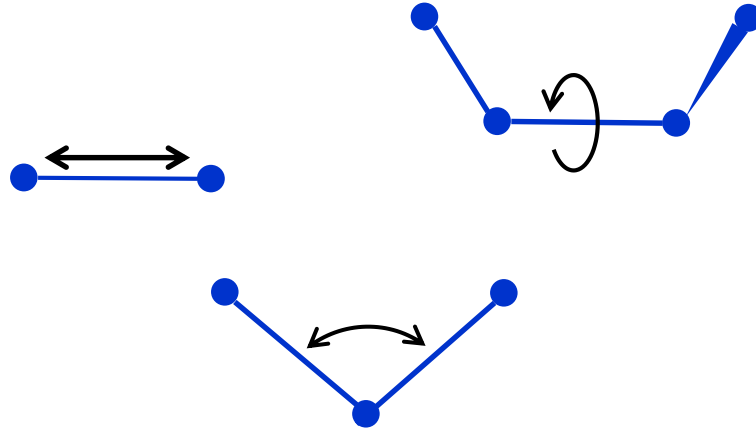
different kinds of motions (smaller)

Bond stretching, angle bending

- nearly harmonic

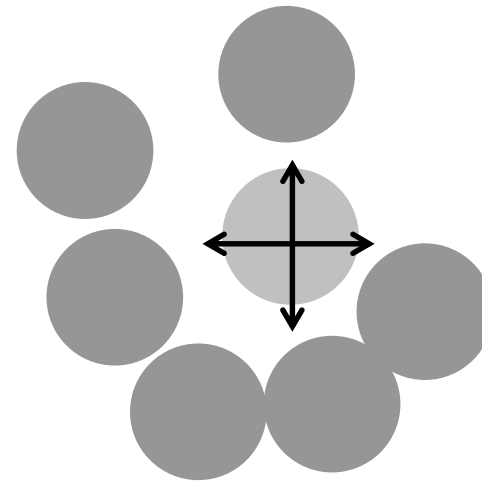
Torsion angles

- separate energy wells



Other motions may be locally like harmonic

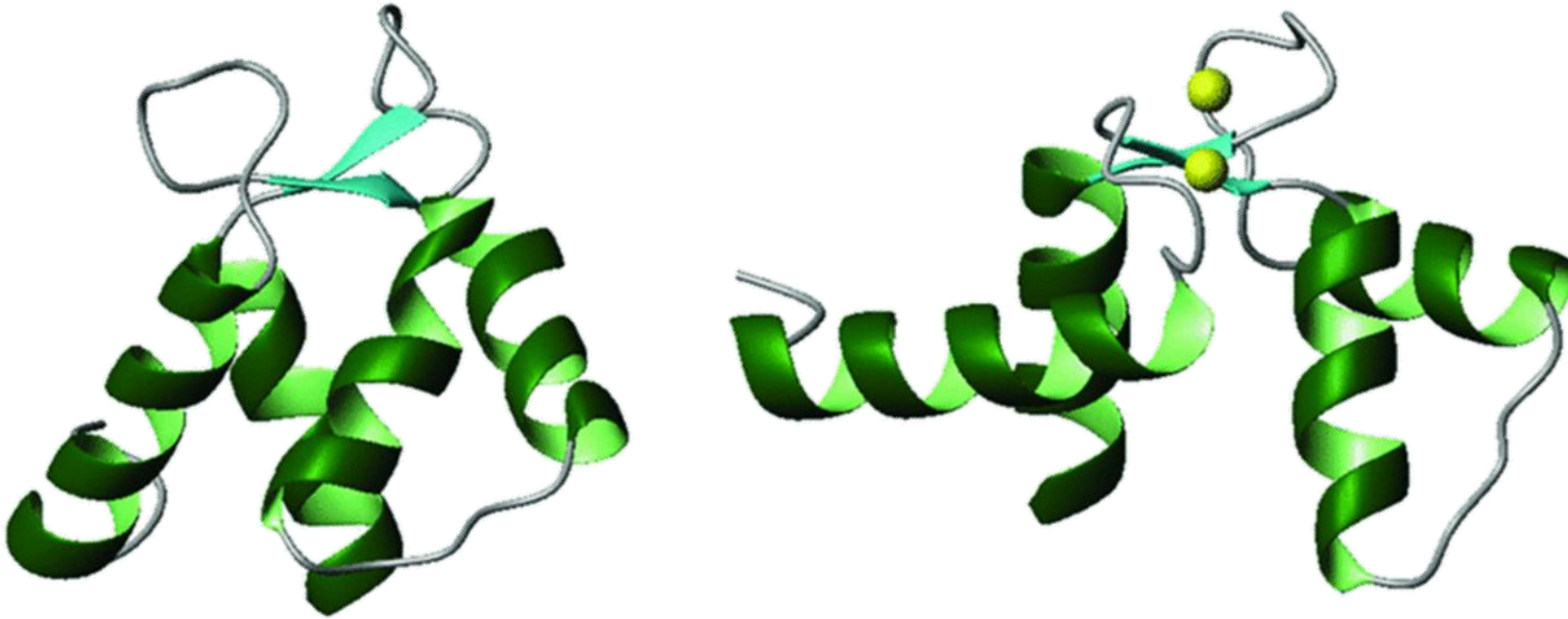
- vibrations of packed atoms



Bigger motions

Calmodulin example

- many Å and probably rather slow
- too move from one conformation to the next – many barriers



Summary

Models are too simple

- most energy terms are not kx^2
 - locally not a bad approximation
- we do not have simple energy barriers
- many more than two states
 - spectrum of motions
- many motions are a mixture (concerted)

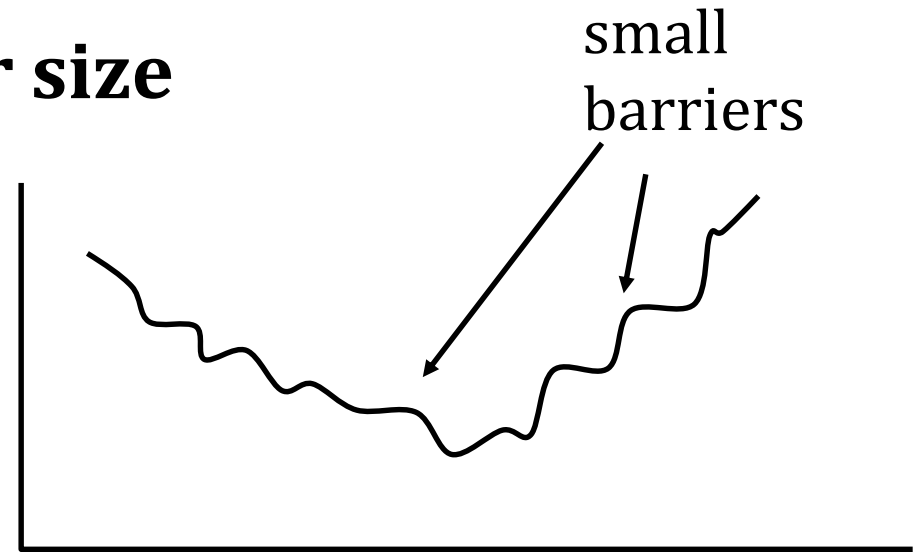
Detection of states

- Are all the different structures present at room temperature ?
- I have two states A and B $\frac{p_a}{p_b} = \exp(E_A - E_B / kT)$
 - if $E_A - E_B$ much bigger than kT (some kJ mol⁻¹)
 - only one state will be seen

Barrier size

Barriers very small

- all particles have plenty of energy
- effectively not present
- may be the case for some rotations



Types of motions

motion	amplitude Å	\log_{10} of time (s)
bond vibration	0.01 – 0.1	-14 to -13
sidechain rotation surface sidechains	5 – 10	-11 to -10
protein hinge bending	1 – 50	-11 to -7
sidechain rotation inside protein	5	-4 to 0
helix / strand breakage	5 – 10	-5 to 1

Summary

- Motions are necessary to explain chemistry
- NMR and X-ray structures are time averages
- usually
 - small motions fast
 - big movements slow
- temperature dependence
 - different for different kinds of movement
 - can be used to estimate energy barriers